

Bluespec-7: Semantics of Bluespec

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<http://csg.csail.mit.edu/6.375/>

L13-1

Topics

- ◆ Guarded actions versus Conditional actions
- ◆ Naming expressions: the “let” statement
- ◆ Modules and methods with implicit conditions
- ◆ Rule composition

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L13-2

BS₀ : A simple language of Guarded Atomic Actions

a is an Action;
e is an Expression;
r is a register (state variable)

action a is guarded by predicate e

conditional action

compound atomic action

$a ::= r := e \mid a \text{ when } e \mid \text{if } e \text{ then } a \mid a ; a$
 $e ::= r \mid c \mid \text{Op}(e, e) \mid e ? e : e \mid e \text{ when } e \mid \dots$

conditional expression

guarded expression

“;” is commutative and associative, i.e.

$a1 ; a2 = a2 ; a1$

$a1 ; (a2 ; a3) = (a1 ; a2) ; a3$

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L13-3

BS₀ Program

A program is a collection of registers and rules:

R, R1, R2, ... are names for rules;
r, r1, r2, ... are register names

Program ::=

Registers r_1, \dots ;

Rule $R_1 a_1 ; \dots ; \text{Rule } R_m a_m ;$

$a ::= r := e \mid a \text{ when } e \mid \text{if } e \text{ then } a \mid a ; a$

$e ::= r \mid c \mid \text{Op}(r_a, r_b) \mid e ? e : e \mid e \text{ when } e \mid \dots$

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L13-4

Guards vs If's

- ◆ A guard on one action of a group of actions affects every action within the group
(a1 when p1); (a2 when p2)
==> (a1; a2) when p1 & p2
- ◆ A condition of a Conditional action only affects the actions within the scope of the conditional action
(if p1 then a1); (if p2 then a2)
p1 has no effect on a2 ...

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L13-5

Canonicalizing BS_0 ignoring guards on expressions

Rules for canonicalization:

1. (a1 when p); a2
==> (a1; a2) when p
2. (a when p1) when p2
==> a when (p1 & p2)
3. if p then (a when q)
==> (if p then a) when (p&q | !p)

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L13-6

Conditionals & Cases

- ◆ if p then a1 else a2
= if p then a1; if !p then a2
- ◆ Similarly for cases

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L13-7

BS_0 : Canonical form

In the canonical form, expressions have no guards and an (or a compound) action has at most one guard and it occurs at the top level;

move all the
guards to the
top level

ag is an Action with guard
a is an Action without guard;
e is an Expression;
r is a register (state variable)

ag ::= a when e
a ::= r := e | if e then a | a ; a
e ::= r | c | Op(e, e) | e ? e : e | ...

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L13-8

Rules for Canonicalizing BS_0

- 1. $(a1 \text{ when } p); a2 \quad \implies (a1; a2) \text{ when } p$
- 2.1 $(a \text{ when } p) \text{ when } q \quad \implies a \text{ when } (p \ \& \ q)$
- 2.2 $(e \text{ when } p) \text{ when } q \quad \implies e \text{ when } (p \ \& \ q)$
- 3.1 $\text{if } p \text{ then } (a \text{ when } q) \quad \implies (\text{if } p \text{ then } a) \text{ when } (p \ \& \ q \ | \ !p)$
- 3.2 $p \ ? \ (e1 \text{ when } q) : e2 \quad \implies (p \ ? \ e1 : e2) \text{ when } (p \ \& \ q \ | \ !p)$
- 3.3 $p \ ? \ e1 : (e2 \text{ when } q) \quad \implies (p \ ? \ e1 : e2) \text{ when } (p \ | \ !p \ \& \ q)$
- 4 $r := (e \text{ when } q) \quad \implies (r := e) \text{ when } q$
- 5.1 $Op(e1 \text{ when } q, e2) \quad \implies Op(e1, e2) \text{ when } q$
- 5.2 $Op(e1, e2 \text{ when } q) \quad \implies Op(e1, e2) \text{ when } q$
- 5.3 $\text{if } (p \text{ when } q) \text{ then } a \quad \implies (\text{if } p \text{ then } a) \text{ when } q$
- 5.4 $(p \text{ when } q) \ ? \ e1 : e2 \quad \implies (p \ ? \ e1 : e2) \text{ when } q$

Theorem: Canonical form for an action exists and is unique up to the boolean simplification of the guard expression.

$BS_1 = BS_0 +$ Let blocks Introducing local names

t, t_1, t_2, \dots are identifiers (not registers)

Program ::=

Registers r_1, \dots, r_n ;

$t_1 = e_1; \dots; t_n = e_n$;

Rule $R_1 a_1; \dots; \text{Rule } R_m a_m$;

$a ::= r := e \ | \ a \text{ when } e \ | \ \text{if } e \text{ then } a \ | \ a ; a$
 $\quad \quad \quad | \ (t_1 = e_1; \dots; t_n = e_n; \text{ in } a)$

$e ::= r \ | \ c \ | \ Op(r_a, r_b) \ | \ e \ ? \ e : e \ | \ e \text{ when } e \ | \ \dots$
 $\quad \quad \quad | \ t \ | \ (t_1 = e_1; \dots; t_n = e_n; \text{ in } e)$

BS_1 Lifting rules

- ◆ Unique local names (t_1, t_2, \dots) can be introduced anywhere for sharing
 $e \implies (t = e \text{ in } t)$
- ◆ Lifting rules for actions
 - $r := (t = e \text{ in } e') \quad \implies (t = e \text{ in } r := e')$
 - $a \text{ when } (t = e \text{ in } e') \quad \implies (t = e \text{ in } (a \text{ when } e'))$
 - $(t = e \text{ in } (e' \text{ when } p)) \quad \implies (t = e \text{ in } e') \text{ when } p$
 - $\text{if } (t = e \text{ in } p) \text{ then } e1 \quad \implies (t = e \text{ in } (\text{if } p \text{ then } e1))$
 - $(t = e \text{ in } a1); a2 \quad \implies (t = e \text{ in } (a1; a2))$
 - $(t1 = e1 \text{ in } (t2 = e2 \text{ in } a)) \quad \implies (t1 = e1; t2 = e2 \text{ in } a)$

Some renaming of local variables may be required
- ◆ Substitution & when clauses
 - $(t = e \text{ when } p \text{ in } e') \implies (t = e; t1 = p \text{ in } [(t \text{ when } t1)/t]e')$
- ◆ Lifting rules for expressions are similar

Lifting lets to the top level

Registers r_1, \dots, r_n ;

$t_1 = e_1; \dots; t_n = e_n$;

Rule $R_1 a_1; \dots; \text{Rule } R_m a_m$;

Rule $R_i (t_{i1} = e_{i1}; \dots; t_{in} = e_{in}; \text{ in } a_i)$

\implies Registers r_1, \dots, r_n ;

$t_1 = e_1; \dots; t_n = e_n$;

$t_{i1} = e_{i1}; \dots; t_{in} = e_{in}$;

Rule $R_1 a_1; \dots; \text{Rule } R_m a_m$;

Rule $R_i a_i$

Some renaming of local variables may be required

BS₁: Canonical form

Program ::=
Registers r_1, \dots ;
 $t_1 = e_1; \dots; t_n = e_n$;
Rule $R_1 ac_1; \dots$; Rule $R_m ac_m$;

$ac ::= (t_1 = e_1; \dots; t_n = e_n; \text{in } aw)$

$ac' ::= (t_1 = e_1; \dots; t_n = e_n; \text{in } a)$

$aw ::= a \mid a \text{ when } e$

$a ::= r := e \mid \text{if } e \text{ then } ac' \mid a ; a$

$ec ::= (t_1 = e_1; \dots; t_n = e_n; \text{in } ew)$

$ec' ::= (t_1 = e_1; \dots; t_n = e_n; \text{in } e)$

$ew ::= e \mid e \text{ when } p$

$e ::= r \mid c \mid \text{Op}(r_a, r_b) \mid e ? ec' : ec' \dots \mid t$

BS₂ = BS₁ + Modules

A program is a collection of (instantiated) modules m, m_1, \dots ;

A module is a collection of rules and interface methods

f, f_1, f_2, \dots are names for “read methods”

g, g_1, g_2, \dots are names for “action methods”

$a ::= r := e \mid a \text{ when } e \mid \text{if } e \text{ then } a \mid a ; a \mid (t = e \text{ in } a)$
 $\mid m.g(e)$

$e ::= r \mid c \mid \text{Op}(r_a, r_b) \mid e ? e : e \mid \dots \mid e \text{ when } e$
 $\mid t \mid (t = e \text{ in } e) \mid m.f(e)$

BS₂ Program

A program is a collection of instantiated modules:

Program ::= $m_1 ; m_2 ; m_2 ; \dots$

Module ::=

Module name

[Register r]

[Rule $R a$];

Interface

Interface ::= [action method]; [read method]

action method ::= **method $g(x) = a$**

read method ::= **method $f(x) = e$**

Implicit conditions

◆ Every method has two parts: guard and body. These will be designated by subscripts G and B , respectively

◆ Making guards explicit in every method call:

$m.h(e) ==>$

$(p = m.h_G \text{ in } m.h_B(e) \text{ when } p)$

BS₂ : Additional Lifting rules

- ◆ Only read methods can be named in a let block
 $m.f(e) \implies (t=m.f(e) \text{ in } t)$
- ◆ $m.g(t = e \text{ in } e') \implies (t = e \text{ in } m.g(e'))$
- ◆ $m.g(e \text{ when } p) \implies m.g(e) \text{ when } p$
 - similar rules for read methods

Some subtle issues

- ◆ Does it matter if we first make the guards explicit and then lift or can we lift at any stage?

BS₂ : Canonicalization procedure

1. Make guards of method calls explicit
2. Lift *lets* to the top
3. Get rid of the *whens* from the *lets*
4. Lift *whens* to the top

Getting ready for circuit generation

- ◆ We need to collect multiple conditional assignments to one register in one expression, i.e.,
 - ... if p1 then r := e1;
if p2 then r := e2;
(r := p3? e4: e5); ...

Notation for conditional assignment

- ◆ $r := e1.p1 + \dots + en.pn$
where
 - $e1, e2, \dots$ are expressions
 - $p1, p2, \dots$ are booleans
- ◆ $e.p$ evaluates to e if p is true otherwise to False (zero's)
- ◆ if p 's are not pairwise mutually exclusive then the program is illegal
- ◆ $e1.p1 + \dots + en.pn$ evaluates to some e_i or if all p 's are false then the value of r does not change

Collecting conditional assignments to a register

- ◆ Apply the following rules after the guards have been made explicit and the program has been canonicalized,
 1. if p then a $\implies a . p$
 - 2.1 $(r := e) . p$ $\implies r := e . p$
 - 2.2 $m.g(e) . p$ $\implies m.g(e . p)$
 3. $(a1; a2) . p$ $\implies a1 . p ; a2 . p$
 - 4.1 $r := e1 ; r := e2$ $\implies r := e1 + e2$
 - 4.2 $m.g(e1); m.g(e2)$ $\implies m.g(e1 + e2)$

Theorem: After applying the above rules to a Program in canonical form any action in it will be reduced the following form:

$r1 := e1; r2 := e2; \dots$

$m.g(e); m1.g1(e1); \dots$ where e 's may contain "." and "+"