6.5900 Computer System Architecture

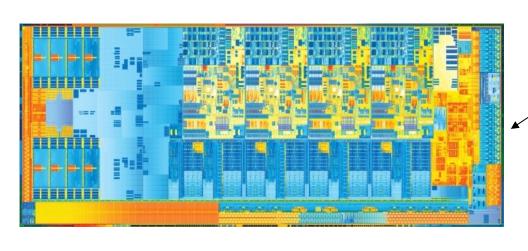
Instructors: Daniel Sanchez

Mengjia Yan

TAs: Hyung Ryong (Ryan) Lee

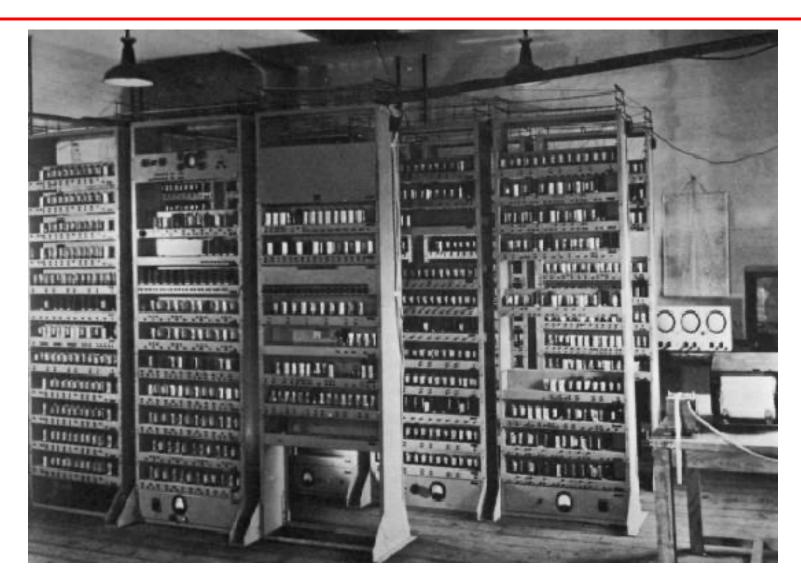
Nikola Samardzic

The processor you built in 6.1910



What you'll understand after taking 6.5900

Computing devices then...



Computing devices now









A journey through this space

What do computer architects actually do?

A journey through this space

- What do computer architects actually do?
- Illustrate via historical examples
 - Early days: ENIAC, EDVAC, and EDSAC
 - Arrival of IBM 650 and then IBM 360
 - Seymour Cray CDC 6600, Cray 1
 - Microprocessors and PCs
 - Multicores
 - Cell phones

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 - Seymour Cray CDC 6600, Cray 1
 - Microprocessors and PCs
 - Multicores
 - Cell phones
- Focus on ideas, mechanisms, and principles, especially those that have withstood the test of time

Application

Algorithm

Programming Language

Operating System/Virtual Machine

Instruction Set Architecture (ISA)

Microarchitecture

Register-Transfer Level (RTL)

Circuits

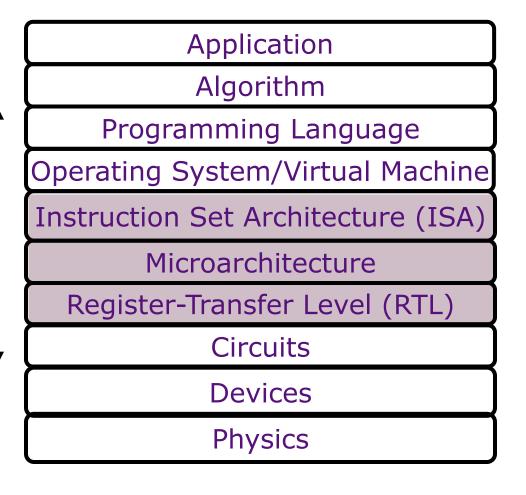
Devices

Physics

Application Algorithm Programming Language Original Operating System/Virtual Machine domain of Instruction Set Architecture (ISA) the computer Microarchitecture architect Register-Transfer Level (RTL) ('50s-'80s) Circuits Devices **Physics**

Application Algorithm Programming Language Original Operating System/Virtual Machine domain of Instruction Set Architecture (ISA) the Domain of computer computer Microarchitecture architect architecture ('90s) Register-Transfer Level (RTL) ('50s-'80s) Circuits Devices **Physics**

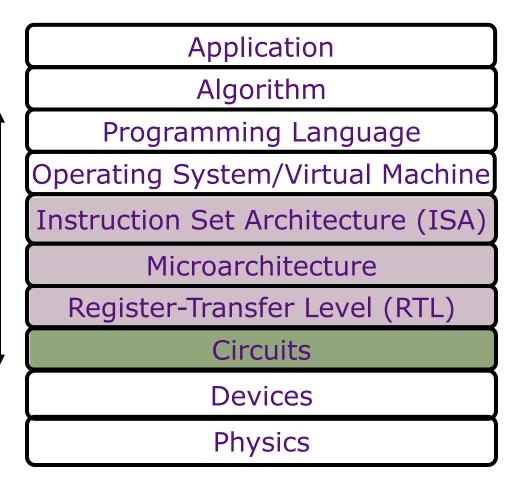
Original domain of the computer architect (`50s-`80s)



Domain of computer architecture ('90s)

Expansion of computer architecture, mid-2000s onward

Original domain of the computer architect ('50s-'80s)

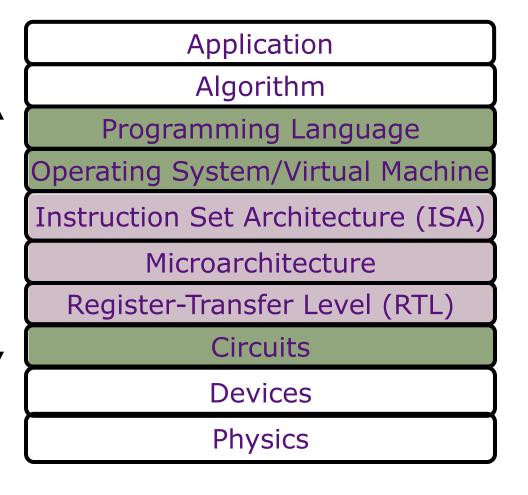


Domain of computer architecture ('90s)

Reliability, power

Expansion of computer architecture, mid-2000s onward

Original domain of the computer architect ('50s-'80s)



Parallel computing, specialization, security, ...

Domain of computer architecture ('90s)

Reliability, power

Expansion of computer architecture, mid-2000s onward

Computer Architecture is the design of abstraction layers

Computer Architecture is the design of abstraction layers

- What do abstraction layers provide?
 - Environmental stability within generation
 - Environmental stability across generations
 - Consistency across a large number of units

Computer Architecture is the design of abstraction layers

What do abstraction layers provide?

- Environmental stability within generation
- Environmental stability across generations
- Consistency across a large number of units

What are the consequences?

- Encouragement to create reusable foundations:
 - Toolchains, operating systems, libraries
- Enticement for application innovation

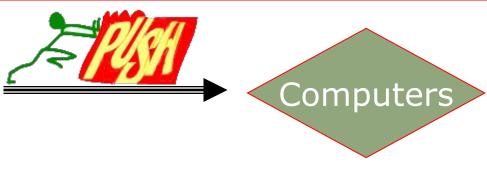
Technology

Transistors
Integrated circuits
VLSI (initially)
Flash memories, ...



Technology

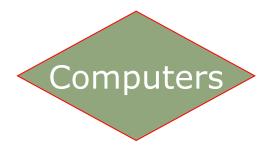
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Technology

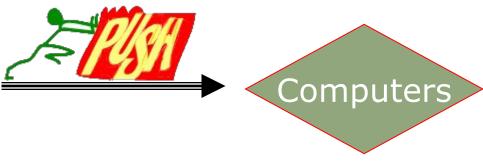
Core memories Magnetic tapes Disks





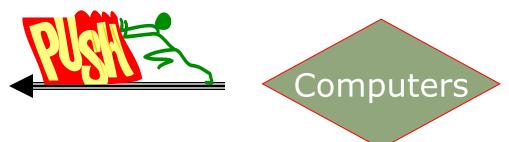
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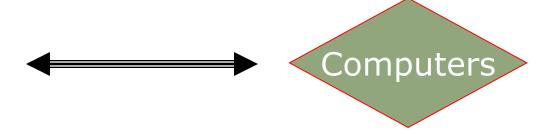
Technology

Core memories Magnetic tapes Disks



Technology

ROMs, RAMs VLSI Packaging Low Power



As people write programs and use computers, our understanding of *programming* and *program behavior* improves.

This has profound though slower impact on computer architecture

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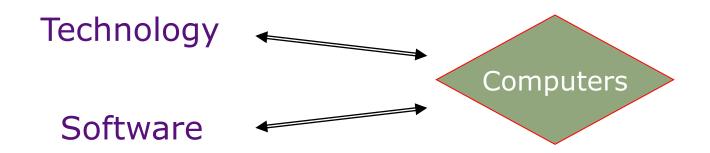
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Modern architects must pay attention to software and compilation issues.

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- Performance of whole system on target applications
 - Average case & worst case

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 - Becoming a limiting factor in many situations, fewer unique chips can be justified

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- Cost to develop applications and system software
 - Often the dominant constraint for any programmable device

Factors to consider:

- Performance of whole system on target applications
 - Average case & worst case
- Cost of manufacturing chips and supporting system
- Power to run system
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- Reliability of system
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At different times, and for different applications at the same point in time, the relative balance of these factors can result in widely varying architectural choices

Course Information

All info kept up to date on the website:

http://csg.csail.mit.edu/6.5900

Contact times

- Lectures on Monday and Wednesday
 - 1:00pm to 2:30pm in room 32-141
- Tutorial on Friday
 - 1:00pm to 2:00pm in room 32-141
 - Attendance is optional
 - Additional tutorials will be held in evenings before quizzes
- Quizzes on Friday (except last quiz)
 - 1:00pm to 2:30pm in room 32-141
 - Attendance is NOT optional
- Instructor office hours
 - After class or by email appointment
- TA office hours
 - Wednesday 4:00-5:30 pm @ Stata 7th floor lounge

Online resources

- We use Piazza extensively
 - Fastest way to get your questions answered
 - All course announcements are made on Piazza

The course has three modules

Module 1

- ISA and Simple In-Order Pipelines
- Caches and Virtual Memory
- Complex Pipelining and Out-of-Order Execution
- Branch Prediction and Speculative Execution

Module 2

- Multithreading and Multiprocessors
- Coherence and consistency
- On-chip networks

Module 3

- Microcoding and VLIW
- Vector machines and GPUs
- Hardware accelerators
- Hardware security

Textbook and readings

- "Computer Architecture: A Quantitative Approach", Hennessy & Patterson, 6th ed.
 - 5th edition available online through MIT Libraries
 - Recommended, but not necessary
 - NOTE: 6th edition (and 6.5900) uses RISC-V as the main ISA;
 prior editions (and 6.5900/6.86 offerings) use MIPS

 Course website lists H&P reading material for each lecture, and optional readings that provide more in-depth coverage

Grading

- Grades are not assigned based on a predetermined curve
 - Most of you are capable of getting an A
- 75% of the grade is based on three closed book
 1.5 hour quizzes
 - The first two quizzes will be held during the tutorials; the last one during the last lecture (dates on web syllabus)
 - We'll have makeups if needed
- 25% of the grade is based on four laboratory exercises
- No final exam
- No final project

Problem sets & labs

Problem sets

- One problem set per module, not graded
- Intended for private study and for tutorials to help prepare for quizzes
- Quizzes assume you are very familiar with the content of problem sets

Labs

- Four graded labs
- Based on widely-used PIN tool
- Labs 2 and 4 are open-ended challenges

You must complete labs & quizzes individually

Please review the collaboration & academic honesty policy

Self evaluation take-home quiz

- Goal is to help you judge for yourself whether you have prerequisites for this class, and to help refresh your memory
- We assume that you understand digital logic, a simple 5-stage pipeline, and simple caches
- Please work by yourself on this quiz not in groups
- Remember to complete self-evaluation section at end of the quiz
- Due by Friday (on recitation or send answers to TA mailing list)

Please contact us if you have concerns about your ability to take the class

Early Developments: From ENIAC to the mid 50's

Prehistory

- 1800s: Charles Babbage
 - Difference Engine (conceived in 1823, first implemented in 1855 by Scheutz)
 - Analytic Engine, the first conception of a general-purpose computer (1833, never implemented)
- 1890: Tabulating machines
- Early 1900s: Analog computers
- 1930s: Early electronic (fixed-function) digital computers

Electronic Numerical Integrator and Computer (ENIAC)

- Designed and built by Eckert and Mauchly at the University of Pennsylvania during 1943-45
- The first, completely digital, electronic, operational, general-purpose analytical calculator!
 - 30 tons, 72 square meters, 200KW
- Performance
 - Read in 120 cards per minute
 - Addition took 200 μs, Division 6 ms
- Not very reliable!

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WW-2 Effort

Application: Ballistic calculations



Electronic Discrete Variable Automatic Computer (EDVAC)

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 - Sequences of instructions were executed independently of the results of the calculation
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 - Solution was the stored program computer
 - ⇒ "program can be manipulated as data"

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- First Draft of a report on EDVAC was published in 1945, but just had von Neumann's signature!
 - Without a doubt the most influential paper in computer architecture

Program = A sequence of instructions

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How to control instruction sequencing?

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manual control calculators

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automatic control external (paper tape)

Harvard Mark I, 1944

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Zuse's Z1, WW2

internal

plug board ENIAC 1946

read-only memory ENIAC 1948

read-write memory EDVAC 1947 (concept)

 The same storage can be used to store program and data

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Calculators

Harvard Mark I, 1944

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ENIAC 1946 ENIAC 1948

EDVAC 1947 (concept)

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EDSAC 1950 Maurice Wilkes

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The Spread of Ideas

ENIAC & EDVAC had immediate impact

brilliant engineering: Eckert & Mauchly

lucid paper: Burks, Goldstine & von Neumann

IAS	Princeton	46-52	Bigelow
EDSAC	Cambridge	46-50	Wilkes
MANIAC	Los Alamos	49-52	Metropolis
JOHNIAC	Rand	50-53	•
ILLIAC	Illinois	49-52	
	Argonne	49-53	
SWAC	UCLA-NBS		

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UNIVAC - the first commercial computer, 1951

Alan Turing's direct influence on these developments is often debated by historians.

Dominant Technology Issue: Reliability

ENIAC

18,000 tubes 20 10-digit numbers **EDVAC**

4,000 tubes 2000 word storage mercury delay lines

Mean time between failures (MTBF)

MIT's Whirlwind with an MTBF of 20 min. was perhaps the most reliable machine!

Reasons for unreliability:

- 1. Vacuum tubes
- 2. Storage medium
 Acoustic delay lines
 Mercury delay lines
 Williams tubes
 Selections

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CORE

J. Forrester

1954

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 - ⇒ Instruction execution time was totally dominated by the memory reference time
- The ability to design complex control circuits to execute an instruction was the central design concern as opposed to the speed of decoding or an ALU operation
- Programmer's view of the machine was inseparable from the actual hardware implementation

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Accumulator-based computing

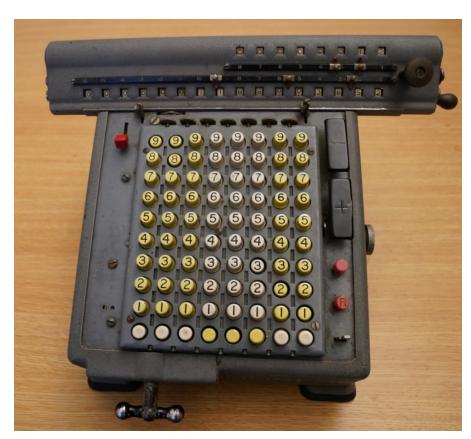


Photo: Joel Emer

• Single Accumulator

 Calculator design carried over to computers

Accumulator-based computing

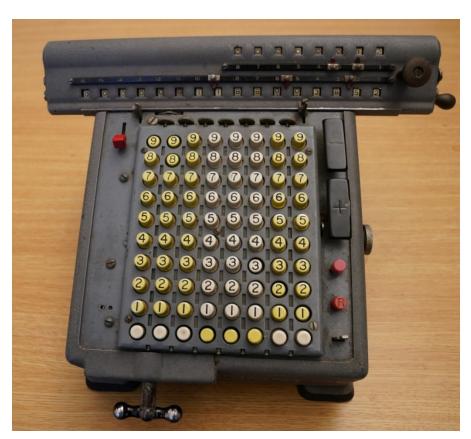


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Why?

Accumulator-based computing



Photo: Joel Emer

• Single Accumulator

 Calculator design carried over to computers

Why?

Registers expensive

Burks, Goldstine & von Neumann ~1946

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Burks, Goldstine & von Neumann ∼1946

LOAD	X
STORE	X

$$AC \leftarrow M[x]$$

 $M[x] \leftarrow (AC)$

$$AC \leftarrow (AC) + M[x]$$

$$AC \leftarrow 2 \times (AC)$$

Burks, Goldstine & von Neumann ∼1946

LOAD	X	$AC \leftarrow M[x]$
STORE	X	$M[x] \leftarrow (AC)$

ADD
$$x$$
 $AC \leftarrow (AC) + M[x]$ SUB x

SHIFT LEFT AC
$$\leftarrow$$
 2 × (AC)
SHIFT RIGHT

JUMP
$$x$$
 $PC \leftarrow x$ $f(AC) \ge 0$ then $PC \leftarrow x$

Burks, Goldstine & von Neumann ∼1946

STORE ADR

X

LOAD STORE	x x	$AC \leftarrow M[x]$ $M[x] \leftarrow (AC)$
ADD SUB	X X	$AC \leftarrow (AC) + M[x]$
MUL DIV	X X	Involved a quotient register
SHIFT LEFT SHIFT RIGHT		AC ← 2 × (AC)
JUMP JGE	X X	$PC \leftarrow x$ if $(AC) \ge 0$ then $PC \leftarrow x$
LOAD ADR	×	$AC \leftarrow Extract address field(M[x])$

The Earliest Instruction Sets

Burks, Goldstine & von Neumann ∼1946

LOAD STORE	X X	$AC \leftarrow M[x]$ $M[x] \leftarrow (AC)$
ADD SUB	X X	$AC \leftarrow (AC) + M[x]$
MUL DIV	X X	Involved a quotient register
SHIFT LEFT SHIFT RIGHT		$AC \leftarrow 2 \times (AC)$
JUMP JGE	X X	$PC \leftarrow x$ if $(AC) \ge 0$ then $PC \leftarrow x$
LOAD ADR STORE ADR	X X	$AC \leftarrow Extract \ address \ field(M[x])$

Typically less than 2 dozen instructions!

C_{i}	$\leftarrow A_i + B_i$	$1 \le i \le n$	А	
LOOP:	JGE	N DONE	В	
F1: F2:	ADD STORE LOAD ADD	ONE N A B	С	
F3:	STORE JUMP	C LOOP	N ONE	-n 1
DONE:	HLT		code	

Problem

C _i	$\leftarrow A_i + B_i$	$1 \le i \le n$	Α	
LOOP:		N	В	
F1:	JGE ADD STORE LOAD	DONE ONE N A	С	
F2: F3:	ADD STORE JUMP	B C LOOP	N ONE	-n 1
DONE:	HLT		code	

$C_i \leftarrow A_i + B_i, 1 \le i \le i$	n A
LOOP: LOAD N	В
JGE DONE ADD ONE STORE N	С
F1: LOAD A F2: ADD B	
F3: STORE C JUMP LOOP	N -n ONE 1
DONE: HLT	
Problem? How to modify the addresses A, B and	code

LOOP	LOAD	N
	JGE	DONE
	ADD	ONE
	STORE	N
F1	LOAD	Α
F2	ADD	В
F3	STORE	C
	JUMP	LOOP
DONE	HLT	

 $C_i \leftarrow A_i + B_i, \quad 1 \le i \le n$

LOOP	LOAD JGE	N DONE
	ADD	ONE
	STORE	N
F1	LOAD	Α
F2	ADD	В
F3	STORE	C
	JUMP	LOOP
DONE	HLT	

 $C_i \leftarrow A_i + B_i, \quad 1 \leq i \leq n$

modify the program for the next iteration

LOOP F1	LOAD JGE ADD STORE LOAD	N DONE ONE N A
F2	ADD	В
F3	STORE LOAD ADR ADD	F1 ONE
modify the program	STORE ADR LOAD ADR ADD	F1 F2 ONE
for the next iteration	STORE ADR	F2
recration	LOAD ADR	F3
	ADD	ONE
DONE	STORE ADR JUMP HLT	F3 LOOP

 $C_i \leftarrow A_i + B_i, \quad 1 \le i \le n$

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LOOP LOAD N JGE DONE ONE ADD STORE Ν F1 LOAD F2 ADD В F3 STORE LOAD ADR F1 **ADD** ONE

modify the program for the next iteration

DONE

STORE ADR F1 LOAD ADR F2 ONE **ADD** STORE ADR F2 LOAD ADR F3 **ADD** ONE STORE ADR **F**3 JUMP LOOP HLT

 $C_i \leftarrow A_i + B_i, \quad 1 \le i \le n$

Each iteration involves total bookkeeping

instruction fetches

operand fetches

stores

LOOP LOAD N JGE DONE ONE ADD STORE Ν F1 LOAD F2 ADD В F3 STORE LOAD ADR F1 **ADD** ONE STORE ADR F1 modify the LOAD ADR F2 program ONE **ADD** for the next STORE ADR F2 iteration

LOAD ADR

STORE ADR

ADD

JUMP

HLT

DONE

 $C_i \leftarrow A_i + B_i, 1 \le i \le n$

Each iteration involves
total bookkeeping
instruction
fetches 17

operand
fetches
stores

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F3

F3

ONE

LOOP

LOOP LOAD N JGE DONE ONE ADD STORE Ν F1 LOAD F2 ADD В F3 STORE

modify the program for the next iteration

DONE

LOAD ADR F1 **ADD** ONE STORE ADR F1 LOAD ADR F2 ONE **ADD** STORE ADR F2 LOAD ADR F3 **ADD** ONE STORE ADR **F**3 JUMP LOOP HLT

 $C_i \leftarrow A_i + B_i, \quad 1 \le i \le n$

Each iteration involves
total bookkeeping
instruction
fetches 17

operand
fetches 10

stores

LOOP LOAD N
JGE DONE
ADD ONE
STORE N
F1 LOAD A
F2 ADD B
F3 STORE C

modify the program for the next iteration

DONE

STORE	С
LOAD ADR	F1
ADD	ONE
STORE ADR	F1
LOAD ADR	F2
ADD	ONE
STORE ADR	F2
LOAD ADR	F3
ADD	ONE
STORE ADR	F3
JUMP	LOOP
HLT	

 $C_i \leftarrow A_i + B_i, \quad 1 \le i \le n$

Each iteration		ves book- keeping
instruction fetches	17	
operand fetches	10	
stores	5	

LOOP N LOAD JGE DONE **ADD** ONE **STORE** Ν F1 LOAD F2 В ADD CTODE F3

modify the program for the next iteration

DONE

STURE	C
LOAD ADR	F1
ADD	ONE
STORE ADR	F1
LOAD ADR	F2
ADD	ONE
STORE ADR	F2
LOAD ADR	F3
ADD	ONE
STORE ADR	F3
JUMP	LOOP
HLT	

 $C_i \leftarrow A_i + B_i$, $1 \le i \le n$

Each iteration		ves book- keeping
instruction fetches	17	14
operand fetches	10	
stores	5	

LOOP	LOAD	N
	JGE	DONE
	ADD	ONE
	STORE	N
F1	LOAD	Α
F2	ADD	В
F3	STORE	C
	LOAD ADR	F1

modify the program for the next iteration

DONE

LOAD ADR	F1
ADD	ONE
STORE ADR	F1
LOAD ADR	F2
ADD	ONE
STORE ADR	F2
LOAD ADR	F3
ADD	ONE
STORE ADR	F3
JUMP	LOOP
HLT	

	Λ	ı D	1 /:	/ 10
$C_i \leftarrow$	A_{i}	+ B _i ,	\perp \leq 1	\leq n
` ` `		·		

Each iteration		ves book- keeping
instruction fetches	17	14
operand fetches	10	8
stores	5	

LOOP	LOAD	N
	JGE	DONE
	ADD	ONE
	STORE	N
F1	LOAD	Α
F2	ADD	В
F3	STORE	C
	LOAD ADR	F1

modify the program for the next iteration

DONE

STORL	C
LOAD ADR	F1
ADD	ONE
STORE ADR	F1
LOAD ADR	F2
ADD	ONE
STORE ADR	F2
LOAD ADR	F3
ADD	ONE
STORE ADR	F3
JUMP	LOOP
HIT	

 $C_i \leftarrow A_i + B_i, 1 \le i \le n$

Each iteration		ves book- keeping
instruction fetches	17	14
operand fetches	10	8
stores	5	4

LOOP	LOAD	N
	JGE	DONE
	ADD	ONE
	STORE	N
F1	LOAD	Α
F2	ADD	В
F3	STORE	C
	LOAD ADR	F1

modify the program for the next iteration

DONE

LOAD ADR	F1
ADD	ONE
STORE ADR	F1
LOAD ADR	F2
ADD	ONE
STORE ADR	F2
LOAD ADR	F3
ADD	ONE
STORE ADR	F3
JUMP	LOOP
HLT	

 $C_i \leftarrow A_i + B_i, \quad 1 \le i \le n$

Each iteration		ves book- keeping
instruction fetches	17	14
operand fetches	10	8
stores	5	4

Most of the executed instructions are for bookkeeping!

Tom Kilburn, Manchester University, mid 50's

One or more specialized registers to simplify address calculation

Tom Kilburn, Manchester University, mid 50's

One or more specialized registers to simplify address calculation

Modify existing instructions

LOAD x, IX ADD x, IX

x, IX $AC \leftarrow M[x + (IX)]$ x, IX $AC \leftarrow (AC) + M[x + (IX)]$

...

Tom Kilburn, Manchester University, mid 50's

One or more specialized registers to simplify address calculation

Modify existing instructions

LOAD x, IX ADD x, IX

x, IX $AC \leftarrow M[x + (IX)]$ x, IX $AC \leftarrow (AC) + M[x + (IX)]$

...

Add new instructions to manipulate index registers

JZi x, IX

if (IX)=0 then $PC \leftarrow x$

else $IX \leftarrow (IX) + 1$

LOADi x, IX

 $IX \leftarrow M[x]$ (truncated to fit IX)

. . .

Tom Kilburn, Manchester University, mid 50's

One or more specialized registers to simplify address calculation

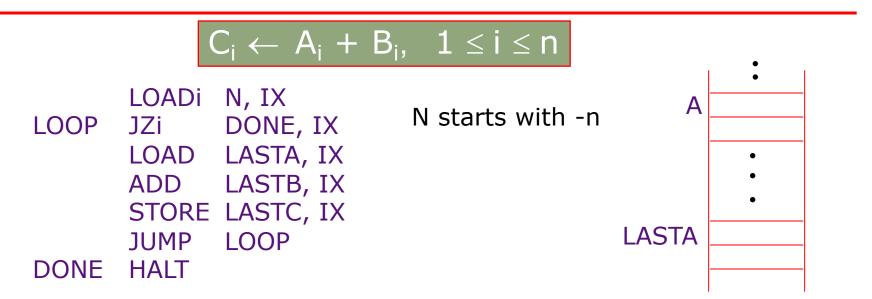
Modify existing instructions

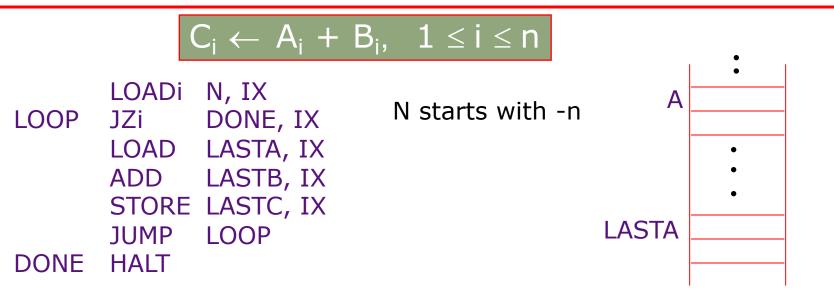
LOAD
$$x$$
, IX $AC \leftarrow M[x + (IX)]$
ADD x , IX $AC \leftarrow (AC) + M[x + (IX)]$

Add new instructions to manipulate index registers

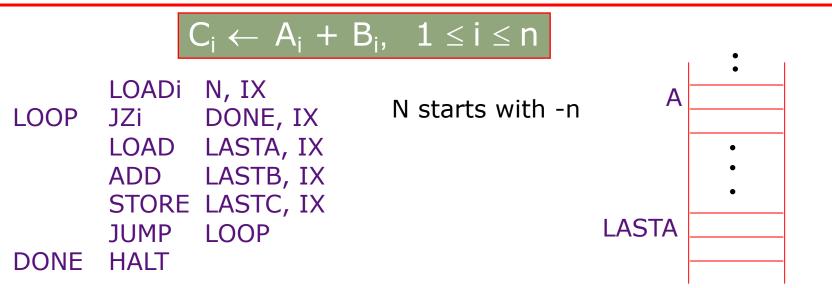
JZi x, IX if
$$(IX)=0$$
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Index registers have accumulator-like characteristics

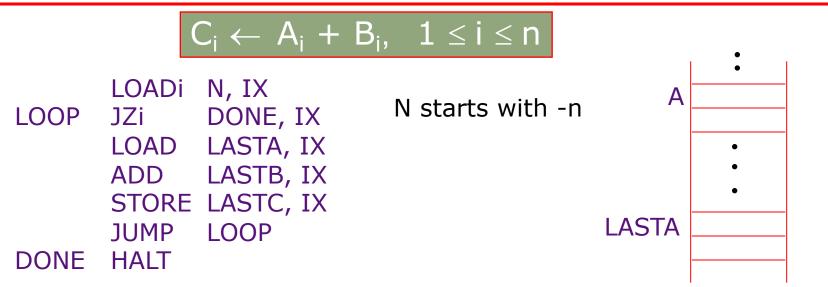




Program does not modify itself

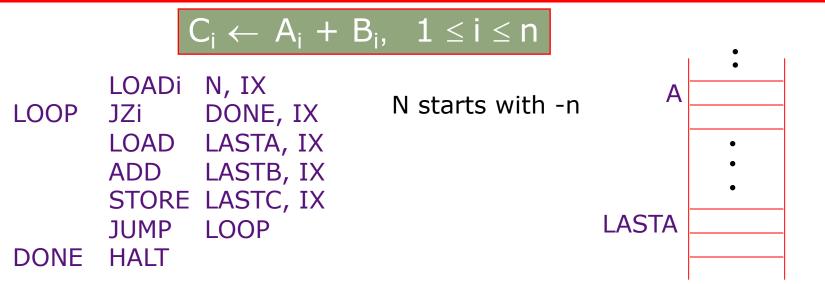


- Program does not modify itself
- Efficiency has improved dramatically (ops / iter)



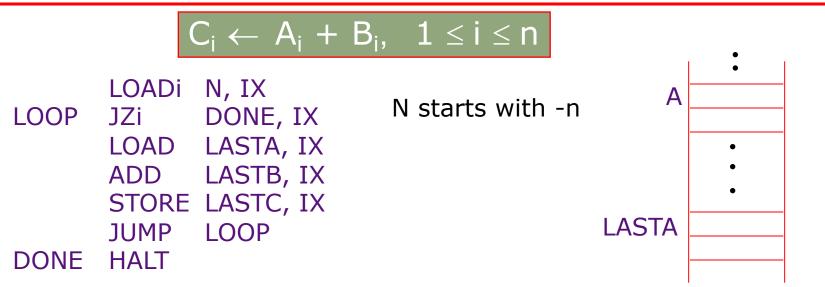
- Program does not modify itself
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```
with index regs without index regs instruction fetch 17 (14) operand fetch 10 (8) store 5 (4)
```



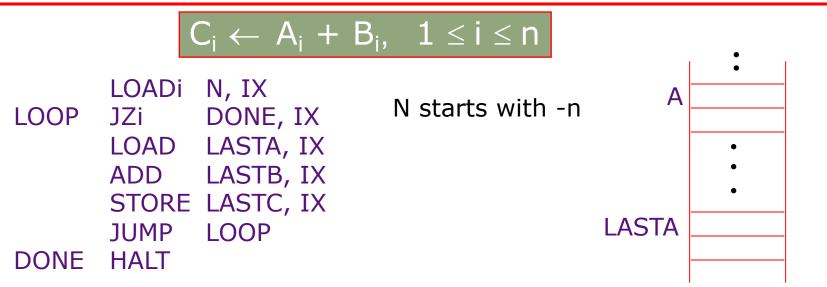
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with index regs without index regs instruction fetch 5(2) 17(14) operand fetch 10(8) store 5(4)
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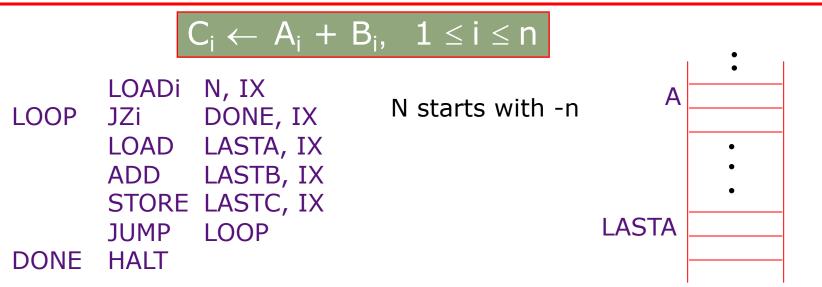
- Program does not modify itself
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```
with index regs without index regs instruction fetch operand fetch 5(2) 17(14) 0 10(8) store 5(4)
```



- Program does not modify itself
- Efficiency has improved dramatically (ops / iter)

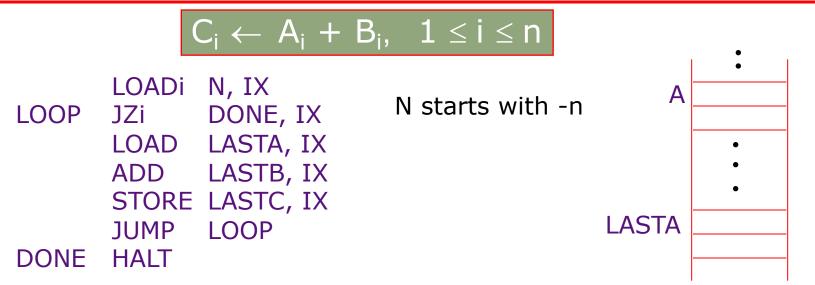
	with index regs	without index regs
instruction fetch	5(2)	17 (14)
operand fetch	2	10 (8)
store	1	5 (4)



- Program does not modify itself
- Efficiency has improved dramatically (ops / iter)

```
with index regs without index regs instruction fetch 5(2) 17 (14) operand fetch 2 10 (8) store 1 5 (4)
```

Costs?



- Program does not modify itself
- Efficiency has improved dramatically (ops / iter)

```
with index regs without index regs instruction fetch 5(2) 17 (14) operand fetch 2 10 (8) store 1 5 (4)
```

- Costs?
- Complex control
- Index register computations (ALU-like circuitry)
- Instructions 1 to 2 bits longer

To increment index register by k

$$AC \leftarrow (IX)$$
 new instruction

$$AC \leftarrow (AC) + k$$

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It may be better to increment IX directly

INCi

$$k$$
, IX $IX \leftarrow (IX) + k$

To increment index register by k

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new instruction
AC \leftarrow (IX)
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 new instruction

also the AC must be saved and restored

It may be better to increment IX directly

$$k$$
, $IX IX \leftarrow (IX) + k$

More instructions to manipulate index register

x, IX
$$M[x] \leftarrow (IX)$$
 (extended to fit a word)

```
To increment index register by k
```

```
AC \leftarrow (IX) new instruction
```

$$AC \leftarrow (AC) + k$$

$$IX \leftarrow (AC)$$
 new instruction

also the AC must be saved and restored

It may be better to increment IX directly

INCi k, IX
$$IX \leftarrow (IX) + k$$

More instructions to manipulate index register

STOREi x, IX
$$M[x] \leftarrow (IX)$$
 (extended to fit a word)

...

IX begins to look like an accumulator

⇒ several index registers several accumulators

⇒ General Purpose Registers

Evolution of Addressing Modes

1. Single accumulator, absolute address

LOAD x

1. Single accumulator, absolute address

LOAD x

2. Single accumulator, index registers

LOAD x, IX

1. Single accumulator, absolute address

LOAD x

2. Single accumulator, index registers

LOAD x, IX

3. Indirection

LOAD (x)

1. Single accumulator, absolute address

2. Single accumulator, index registers

3. Indirection

4. Multiple accumulators, index registers, indirection

```
LOAD R, IX, x or LOAD R, IX, (x) the meaning? R \leftarrow M[M[x] + (IX)] or R \leftarrow M[M[x + (IX)]]
```

1. Single accumulator, absolute address

2. Single accumulator, index registers

3. Indirection

or

4. Multiple accumulators, index registers, indirection

LOAD R, IX, x
LOAD R, IX, (x) the meaning?

$$R \leftarrow M[M[x] + (IX)]$$

or $R \leftarrow M[M[x + (IX)]]$

5. Indirect through registers

LOAD
$$R_I$$
, (R_J)

1. Single accumulator, absolute address

2. Single accumulator, index registers

3. Indirection

or

4. Multiple accumulators, index registers, indirection

LOAD R, IX, x LOAD R, IX, (x) the meaning?
$$R \leftarrow M[M[x] + (IX)]$$

5. Indirect through registers

LOAD
$$R_{I}$$
, (R_{J})

6. The works

LOAD
$$R_I$$
, R_J , (R_K) $R_J = index$, $R_K = base addr$

or $R \leftarrow M[M[x + (IX)]]$

Variety of Instruction Formats

Variety of Instruction Formats

 Three address formats: One destination and up to two operand sources per instruction

```
\begin{array}{ll} \text{(Reg op Reg) to Reg} & R_{\text{I}} \leftarrow (R_{\text{J}}) \text{ op } (R_{\text{K}}) \\ \text{(Reg op Mem) to Reg} & R_{\text{I}} \leftarrow (R_{\text{J}}) \text{ op } M[x] \end{array}
```

- x can be specified directly or via a register
- effective address calculation for x could include indexing, indirection, ...

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```

- x can be specified directly or via a register
- effective address calculation for x could include indexing, indirection, ...
- Two address formats: the destination is same as one of the operand sources

(Reg op Reg) to Reg
$$R_I \leftarrow (R_I)$$
 op (R_J) (Reg op Mem) to Reg $R_I \leftarrow (R_I)$ op $M[x]$

- One address formats: Accumulator machines
 - Accumulator is always other implicit operand

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- Zero address formats: operands on a stack

```
add M[sp-1] \leftarrow M[sp] + M[sp-1]
load M[sp] \leftarrow M[M[sp]]
```

Stack can be in registers or in memoryusually top of stack cached in registers

- One address formats: Accumulator machines
 - Accumulator is always other implicit operand
- Zero address formats: operands on a stack

```
add M[sp-1] \leftarrow M[sp] + M[sp-1] Register SP B E C
```

Memory

- Stack can be in registers or in memory
 - usually top of stack cached in registers

- One address formats: Accumulator machines
 - Accumulator is always other implicit operand
- Zero address formats: operands on a stack

```
add M[sp-1] \leftarrow M[sp] + M[sp-1] Register A B C Memory
```

- Stack can be in registers or in memory
 - usually top of stack cached in registers

Many different formats are possible!

Instruction sets in the mid 50's

 Great variety of instruction sets, but all intimately tied to implementation details

 Programmer's view of the machine was inseparable from the actual hardware implementation!

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Next Lecture: Instruction Set Architectures and Caches