Memory Consistency Models

Mengjia Yan
Computer Science and Artificial Intelligence Lab
M.I.T.
Coherence vs Consistency

- Cache coherence makes private caches invisible to software
  - Concerns reads/writes to a single memory location
Coherence vs Consistency

- Cache coherence makes private caches invisible to software
  - Concerns reads/writes to a single memory location

- Memory consistency models precisely specify how memory behaves with respect to read and write operations from multiple processors
  - Concerns reads/writes to multiple memory locations
### Why Consistency Matters

*Initial memory contents*

<table>
<thead>
<tr>
<th>a</th>
<th>0</th>
</tr>
</thead>
<tbody>
<tr>
<td>flag</td>
<td>0</td>
</tr>
</tbody>
</table>

#### Processor 1

- Store (a), 10;
- Store (flag), 1;

#### Processor 2

- L: Load r1, (flag);
- if r1 == 0 goto L;
- Load r2, (a);

- What value does r2 hold after both processors finish running this code?
Why Consistency Matters

Initial memory contents

a: 0
flag: 0

Processor 1
Store (a), 10;
Store (flag), 1;

Processor 2
L: Load r1, (flag);
if r1 == 0 goto L;
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• What value does r2 hold after both processors finish running this code?

It depends on the order in which processor 2 observes processor 1’s stores!
# Why Consistency Matters

*Initial memory contents*

- `a`: 0
- `flag`: 0

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- What value does `r2` hold after both processors finish running this code?

  It depends on the order in which processor 2 observes processor 1’s stores!

  10 if `Store (flag) > Store (a)`; 0 or 10 otherwise
Sequential Consistency
A Straightforward Memory Model

“A system is sequentially consistent if the result of any execution is the same as if the operations of all the processors were executed in some sequential order, and the operations of each individual processor appear in the order specified by the program”  

Leslie Lamport

Sequential Consistency =

arbitrary order-preserving interleaving
of memory references of sequential programs
Sequential Consistency

- In-order instruction execution
- Atomic loads and stores

**Processor 1**
- Store \((a), 10;\)
- Store \((\text{flag}), 1;\)

**Processor 2**
- L: Load \(r_1, (\text{flag});\)
- if \(r_1 == 0\) goto L;
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Sequential Consistency

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**Processor 1**
- \( \text{Store (a), 10;} \)
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- \( \text{L: Load r1, (flag);} \)
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- L: Load \(r1, (\text{flag});\)
- if \(r_1 == 0\) goto L;
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Sequential Consistency

- In-order instruction execution
- Atomic loads and stores

SC is easy to understand, but architects and compiler writers want to violate it for performance
Memory Model Issues

Architectural optimizations that are correct for uniprocessors often violate sequential consistency and result in a new memory model for multiprocessors.
Consistency Models

• Sequential Consistency
  – All reads and writes in order

• Relaxed Consistency (one or more of the following)
  – Loads may be reordered after loads
    • e.g., PA-RISC, Power, Alpha
  – Loads may be reordered after stores
    • e.g., PA-RISC, Power, Alpha
  – Stores may be reordered after stores
    • e.g., PA-RISC, Power, Alpha, PSO
  – Stores may be reordered after loads
    • e.g., PA-RISC, Power, Alpha, PSO, TSO, x86
  – Other more esoteric characteristics
    • e.g., Alpha
Committed Store Buffers

- CPU can continue execution while earlier committed stores are still propagating through memory system
  - Processor can commit other instructions (including loads and stores) while first store is committing to memory
  - Committed store buffer can be combined with speculative store buffer in an out-of-order CPU

- Local loads can bypass values from buffered stores to same address
Example 1: Store Buffers

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<tr>
<td>Store ((\text{flag}_1)), 1;</td>
<td>Store ((\text{flag}_2)), 1;</td>
</tr>
<tr>
<td>Load (r_1), ((\text{flag}_2));</td>
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Initially, all memory locations contain zeros
**Example 1: Store Buffers**

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**Question:** Is it possible that \(r_1 = 0\) and \(r_2 = 0\)?

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**Question:** Is it possible that \( r_1 = 0 \) and \( r_2 = 0 \)?

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**Question:** Is it possible that \(r\(_1\)=0\) and \(r\(_2\)=0\)?

- **Sequential consistency:** No

- Suppose Loads can go ahead of Stores waiting in the store buffer:

Initially, all memory locations contain zeros
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**Question:** Is it possible that r₁ = 0 and r₂ = 0?

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- **Suppose Loads can go ahead of Stores waiting in the store buffer:** Yes!

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Question: Is it possible that \( r₁ = 0 \) and \( r₂ = 0 \)?

- **Sequential consistency:** No
- **Suppose Loads can go ahead of Stores waiting in the store buffer:** Yes!

Total Store Order (TSO):
Sun SPARC, IBM 370

Initially, all memory locations contain zeros
Example 2: Store-Load Bypassing

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**Question:** Do extra Loads have any effect?
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**Question:** Do extra Loads have any effect?
- **Sequential consistency:** No
- *Suppose Store-Load bypassing is permitted in the store buffer*
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Question: Do extra Loads have any effect?

- **Sequential consistency:** No
- **Suppose Store-Load bypassing is permitted in the store buffer**
  - No effect in Sparc’s TSO model, still not SC
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Question: Do extra Loads have any effect?

- **Sequential consistency**: No
- Suppose **Store-Load bypassing is permitted in the store buffer**
  - No effect in Sparc’s TSO model, still not SC
  - In IBM 370, a load cannot return a written value until it is visible to other processors => implicitly adds a memory fence, looks like SC
Interleaved Memory System

- Achieve greater throughput by spreading memory addresses across two or more parallel memory subsystems
  - In snooping system, can have two or more snoops in progress at same time (e.g., Sun UE10K system has four interleaved snooping busses)
  - Greater bandwidth from main memory system as two memory modules can be accessed in parallel
Example 3: Non-FIFO Store buffers

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Sparc’s PSO memory model
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- **Assuming stores are ordered:** Yes because Loads can be reordered
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Alpha, Sparc’s RMO, PowerPC’s WO
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- Sequential consistency:
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Question: Is it possible that \(r_1=1\) and \(r_2=2\) but \(r_3=2\) and \(r_4=1\)?

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**Question:** Is it possible that \( r₁=1 \) and \( r₂=2 \) but \( r₃=2 \) and \( r₄=1 \) ?

- **Sequential consistency:** No
- **Even if Loads on a processor are ordered, the different ordering of stores can be observed if the Store operation is not atomic.**
### Example 6: Causality

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<td></td>
<td>Store (flag$_2$), 1;</td>
<td>Load r$_3$, (flag$_1$);</td>
</tr>
</tbody>
</table>

Question: Is it possible that $r_1 = 1$ and $r_2 = 1$ but $r_3 = 0$?
Example 6: Causality

<table>
<thead>
<tr>
<th>Process 1</th>
<th>Process 2</th>
<th>Process 3</th>
</tr>
</thead>
<tbody>
<tr>
<td>Store $(\text{flag}_1)$, 1;</td>
<td>Load $r_1$, $(\text{flag}_1)$;</td>
<td>Load $r_2$, $(\text{flag}_2)$;</td>
</tr>
<tr>
<td></td>
<td>Store $(\text{flag}_2)$, 1;</td>
<td>Load $r_3$, $(\text{flag}_1)$;</td>
</tr>
</tbody>
</table>

Question: Is it possible that $r_1 = 1$ and $r_2 = 1$ but $r_3 = 0$?

• Sequential consistency: No
Example 6: Causality

<table>
<thead>
<tr>
<th>Process 1</th>
<th>Process 2</th>
<th>Process 3</th>
</tr>
</thead>
<tbody>
<tr>
<td>Store (flag(_{1})), 1;</td>
<td>Load r(<em>{1}), (flag(</em>{1}));</td>
<td>Load r(<em>{2}), (flag(</em>{2}));</td>
</tr>
<tr>
<td></td>
<td>Store (flag(_{2})), 1;</td>
<td>Load r(<em>{3}), (flag(</em>{1}));</td>
</tr>
</tbody>
</table>

Question: Is it possible that \( r_{1}=1 \) and \( r_{2}=1 \) but \( r_{3}=0 \)?

- **Sequential consistency:** No
- **With load/load reordering:**
Example 6: Causality

<table>
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<tr>
<th>Process 1</th>
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<th>Process 3</th>
</tr>
</thead>
<tbody>
<tr>
<td>Store (flag\textsubscript{1}), 1;</td>
<td>Load r\textsubscript{1}, (flag\textsubscript{1});</td>
<td>Load r\textsubscript{2}, (flag\textsubscript{2});</td>
</tr>
<tr>
<td></td>
<td>Store (flag\textsubscript{2}), 1;</td>
<td>Load r\textsubscript{3}, (flag\textsubscript{1});</td>
</tr>
</tbody>
</table>

Question: Is it possible that r\textsubscript{1}=1 and r\textsubscript{2}=1 but r\textsubscript{3}=0 ?

- **Sequential consistency:** No
- **With load/load reordering:** Yes

Alpha
Example 7: Register Renaming

Initially both $r_1$ and $r_2$ contain 1.

<table>
<thead>
<tr>
<th>Process 1</th>
<th>Process 2</th>
</tr>
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<tbody>
<tr>
<td>Store (flag$_1$), $r_1$;</td>
<td>Store (flag$_2$), $r_2$;</td>
</tr>
<tr>
<td>Load $r_1$, (flag$_2$);</td>
<td>Load $r_2$, (flag$_1$);</td>
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</tbody>
</table>
Example 7: Register Renaming

Initially both $r_1$ and $r_2$ contain 1.

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<td>Store (flag$_1$), $r_1$;</td>
<td>Store (flag$_2$), $r_2$;</td>
</tr>
<tr>
<td>Load $r_1$, (flag$_2$);</td>
<td>Load $r_2$, (flag$_1$);</td>
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</tbody>
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Question: Is it possible that $r_1=0$ but $r_2=0$?
Example 7: Register Renaming

<table>
<thead>
<tr>
<th>Process 1</th>
<th>Process 2</th>
</tr>
</thead>
<tbody>
<tr>
<td>Store (flag₁), r₁;</td>
<td>Store (flag₂), r₂;</td>
</tr>
<tr>
<td>Load r₁, (flag₂);</td>
<td>Load r₂, (flag₁);</td>
</tr>
</tbody>
</table>

Initially both r₁ and r₂ contain 1.

Question: Is it possible that r₁=0 but r₂=0?
- Sequential consistency: No
### Example 7: Register Renaming

Initially both $r_1$ and $r_2$ contain 1.

<table>
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<th>Process 1</th>
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<tr>
<td>Store (flag$_1$), $r_1$;</td>
<td>Store (flag$_2$), $r_2$;</td>
</tr>
<tr>
<td>Load $r_1$, (flag$_2$);</td>
<td>Load $r_2$, (flag$_1$);</td>
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</table>

**Question:** Is it possible that $r_1=0$ but $r_2=0$?

- **Sequential consistency:** No
- **Register renaming:** Yes because it removes anti-dependencies
<table>
<thead>
<tr>
<th><strong>Process 1</strong></th>
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</tr>
</thead>
<tbody>
<tr>
<td>Store (flag₁), ( r₁ );</td>
<td>Store (flag₂), ( r₂ );</td>
</tr>
<tr>
<td>Load ( r₁ ), (flag₂);</td>
<td>Load ( r₂ ), (flag₁);</td>
</tr>
</tbody>
</table>

Initially both \( r₁ \) and \( r₂ \) contain 1.

**Question**: Is it possible that \( r₁ = 0 \) but \( r₂ = 0 \)?

- **Sequential consistency**: No
- **Register renaming**: Yes because it removes anti-depencies
Example 7: Register Renaming

Initially both \( r_1 \) and \( r_2 \) contain 1.

### Process 1

- Store (flag\(_1\)), \( r_1 \);
- Load \( r_1 \), (flag\(_2\));

### Process 2

- Store (flag\(_2\)), \( r_2 \);
- Load \( r_2 \), (flag\(_1\));

**Question:** Is it possible that \( r_1 = 0 \) but \( r_2 = 0 \)?

- **Sequential consistency:** No
- **Register renaming:** Yes because it removes anti-dependencies
Initially both $r_1$ and $r_2$ contain 1.

**Process 1**
- Store (flag$_1$), $r_1$;
- Load $r_1$, (flag$_2$);

**Process 2**
- Store (flag$_2$), $r_2$;
- Load $r_2$, (flag$_1$);

**Question:** Is it possible that $r_1=0$ but $r_2=0$?
- **Sequential consistency:** No
- **Register renaming:** Yes because it removes anti-dependencies
Example 7: Register Renaming

Initially both \( r_1 \) and \( r_2 \) contain 1.

**Process 1**
- Store (flag\(_1\)), \( r_1 \);
- Load \( r_1 \), (flag\(_2\));

**Process 2**
- Store (flag\(_2\)), \( r_2 \);
- Load \( r_2 \), (flag\(_1\));

Register renaming will eliminate this edge

**Question:** Is it possible that \( r_1 = 0 \) but \( r_2 = 0 \)?
- **Sequential consistency:** No
- **Register renaming:** Yes because it removes anti-dependencies
Example 7: Register Renaming

Initially both $r_1$ and $r_2$ contain 1.

**Process 1**
- Store (flag$_1$), $r_1$;
- Load $r_1$, (flag$_2$);

**Process 2**
- Store (flag$_2$), $r_2$;
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Register renaming will eliminate this edge

Question: Is it possible that $r_1=0$ but $r_2=0$?

- **Sequential consistency:** No
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Initially both $r_1$ and $r_2$ contain 1.

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- **Register renaming:** Yes because it removes anti-dependencies
Example 8: Speculative Execution

<table>
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<tr>
<th>Process 1</th>
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<tbody>
<tr>
<td>Store (a), 1;</td>
<td>L: Load $r_1$, (flag);</td>
</tr>
<tr>
<td>Store (flag), 1;</td>
<td>if $r_1 == 0$ goto L;</td>
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<td>Load $r_2$, (a);</td>
</tr>
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</table>
### Example 8: Speculative Execution

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Question: Is it possible that $r_1=1$ but $r_2=0$?

- **Sequential consistency**: No
Example 8: Speculative Execution

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<th>Process 1</th>
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<tr>
<td>Store (a), 1;</td>
<td>L: Load r₁, (flag);</td>
</tr>
<tr>
<td>Store (flag), 1;</td>
<td>if r₁ == 0 goto L;</td>
</tr>
<tr>
<td></td>
<td>Load r₂, (a);</td>
</tr>
</tbody>
</table>

Question: Is it possible that \( r₁ = 1 \) but \( r₂ = 0 \)?

- Sequential consistency: No
- With speculative loads: Yes even if the stores are ordered
Example 9: Address Speculation

Initially both $r_1$ and $r_3$ contain 1.

**Process 1**

- Store $(\text{flag}_1), r_1$;
- Load $r_2, (\text{flag}_2)$;

**Process 2**

- Store $(\text{flag}_2), r_3$;
- Load $r_4, (\text{flag}_1)$;

Flag$_1$ and flag$_2$ are registers pointing at memory locations $L_{14}$-$18$. 
Example 9: Address Speculation

Initially both $r_1$ and $r_3$ contain 1.

<table>
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<th>Process 1</th>
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<tbody>
<tr>
<td>Store (flag$_1$), $r_1$;</td>
<td>Store (flag$_2$), $r_3$;</td>
</tr>
<tr>
<td>Load $r_2$, (flag$_2$);</td>
<td>Load $r_4$, (flag$_1$);</td>
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**Question:** Is it possible that $r_2 = 0$ but $r_4 = 0$?

Flag$_1$ and flag$_2$ are registers pointing at memory locations L14-18.
Example 9: Address Speculation

Initially both $r_1$ and $r_3$ contain 1.

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<td>Load $r_2$, (flag$_2$);</td>
<td>Load $r_4$, (flag$_1$);</td>
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</tbody>
</table>

Question: Is it possible that $r_2=0$ but $r_4=0$?

• Sequential consistency: No

Flag$_1$ and flag$_2$ are registers pointing at memory locations L14-18.
Example 9: Address Speculation

<table>
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<th>Process 1</th>
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</thead>
<tbody>
<tr>
<td>Store (flag(_1)), (r_1);</td>
<td>Store (flag(_2)), (r_3);</td>
</tr>
<tr>
<td>Load (r_2), (flag(_2));</td>
<td>Load (r_4), (flag(_1));</td>
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</table>

Initially both \(r_1\) and \(r_3\) contain 1.

**Question:** Is it possible that \(r_2 = 0\) but \(r_4 = 0\)?

- **Sequential consistency:** No
- **Address speculation:** Yes because it removes the dependencies between the stores and loads
Example 9: Address Speculation

<table>
<thead>
<tr>
<th>Process 1</th>
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</thead>
<tbody>
<tr>
<td>Store (flag₁), r₁;</td>
<td>Store (flag₂), r₃;</td>
</tr>
<tr>
<td>Load r₂, (flag₂);</td>
<td>Load r₄, (flag₁);</td>
</tr>
</tbody>
</table>

Initially both r₁ and r₃ contain 1.

Question: Is it possible that r₂=0 but r₄=0?
- Sequential consistency: No
- Address speculation: Yes because it removes the dependencies between the stores and loads

Flag₁ and flag₂ are registers pointing at memory locations.
Example 9: Address Speculation

Initially both $r_1$ and $r_3$ contain 1.

Process 1
- Store (flag$_1$), $r_1$;
- Load $r_2$, (flag$_2$);

Process 2
- Store (flag$_2$), $r_3$;
- Load $r_4$, (flag$_1$);

Question: Is it possible that $r_2=0$ but $r_4=0$?
- **Sequential consistency:** No
- **Address speculation:** Yes because it removes the dependencies between the stores and loads

Flag$_1$ and flag$_2$ are registers pointing at memory locations $L14-L18$. 

*October 25, 2023*
Example 9: Address Speculation

Initially both $r_1$ and $r_3$ contain 1.

**Process 1**
- Store $(\text{flag}_1), r_1$;
- Load $r_2, (\text{flag}_2)$;

**Process 2**
- Store $(\text{flag}_2), r_3$;
- Load $r_4, (\text{flag}_1)$;

**Question:** Is it possible that $r_2=0$ but $r_4=0$?
- **Sequential consistency:** No
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Flag$_1$ and flag$_2$ are registers pointing at memory locations L14-18.
Example 9: Address Speculation

Initially both \( r_1 \) and \( r_3 \) contain 1.

Process 1

- Store (flag\(_1\)), \( r_1 \);
- Load \( r_2 \), (flag\(_2\));

Process 2

- Store (flag\(_2\)), \( r_3 \);
- Load \( r_4 \), (flag\(_1\));

Question: Is it possible that \( r_2 = 0 \) but \( r_4 = 0 \)?
- **Sequential consistency:** No
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\( Flag_1 \) and \( flag_2 \) are registers pointing at memory locations L14-18.
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Initially both $r_1$ and $r_3$ contain 1.

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Flag_1 and flag_2 are registers pointing at memory locations L14-18.
Example 9: Address Speculation

Initially both $r_1$ and $r_3$ contain 1.

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Initially both $r_1$ and $r_3$ contain 1.

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Question: Is it possible that $r_2=0$ but $r_4=0$?

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Flag$_1$ and flag$_2$ are registers pointing at memory locations L14-18
Weaker Memory Models & Memory Fence Instructions

- Architectures with weaker memory models provide memory fence instructions to prevent otherwise permitted re-orderings of loads and stores.

\[
\text{Store } (a_1), \text{ r2;}
\]

\[
\text{Load } r1, (a_2);
\]

Similarly:

The Load and Store can be reordered if \( a_1 \neq a_2 \). Insertion of \( \text{Fence}_{wr} \) will disallow this reordering.
Weaker Memory Models & Memory Fence Instructions

- Architectures with weaker memory models provide memory fence instructions to prevent otherwise permitted re-orderings of loads and stores.

\[ \text{Store} \ (a_1), \ r2; \]
\[ \text{Fence}_{wr} \]
\[ \text{Load} \ r1, \ (a_2); \]

The Load and Store can be reordered if \( a_1 \neq a_2 \). Insertion of \( \text{Fence}_{wr} \) will disallow this reordering.

Similarly:
Weaker Memory Models & Memory Fence Instructions

- Architectures with weaker memory models provide memory fence instructions to prevent otherwise permitted re-orderings of loads and stores

```
Store (a_1), r2;  
Fence_{wr}  
Load r1, (a_2);
```

The Load and Store can be reordered if $a_1 \neq a_2$. Insertion of Fence_{wr} will disallow this reordering

Similarly:

```
Fence_{rr};  
Fence_{rw};  
Fence_{ww};
```
Weaker Memory Models & Memory Fence Instructions

- Architectures with weaker memory models provide memory fence instructions to prevent otherwise permitted re-orderings of loads and stores.

Store \((a_1), r2;\)  
Fence\(_{wr}\)  
Load \(r1, (a_2);\)

The Load and Store can be reordered if \(a_1 \neq a_2\). Insertion of Fence\(_{wr}\) will disallow this reordering.

Similarly: \(\text{Fence}_{rr}; \text{Fence}_{rw}; \text{Fence}_{ww};\)

SUN’s Sparc: \(\text{MEMBAR; MEMBARRR; MEMBARRW; MEMBARWR; MEMBARWW}\)

PowerPC: \(\text{Sync; EIEIO}\)
Enforcing Ordering using Fences

**Processor 1**
- Store (a),10;
- Store (flag),1;

**Processor 2**
- L: Load \( r_1 \), (flag);
- if \( r_1 == 0 \) goto L;
- Load \( r_2 \), (a);
Enforcing Ordering using Fences

Processor 1
Store (a),10;
Store (flag),1;

Processor 2
L: Load r₁, (flag);
   if r₁ == 0 goto L;
   Load r₂, (a);

Processor 1
Store (a),10;
Fence_{ww};
Store (flag),1;

Processor 2
L: Load r₁, (flag);
   if r₁ == 0 goto L;
   Fence_{rr};
   Load r₂, (a);
Weaker (Relaxed) Memory Models
Weaker (Relaxed) Memory Models

- Alpha, Sparc
- PowerPC, ...
- Write buffers
- Store is globally performed
- TSO, PSO, RMO, ...
- SMP, DSM, CMP
- RMO=W0?
Weaker (Relaxed) Memory Models

- Hard to understand and remember
Weaker (Relaxed) Memory Models

- Hard to understand and remember
- Unstable - Modèle de l’année
Weaker (Relaxed) Memory Models

- Hard to understand and remember
- Unstable - *Modèle de l’année*
- Abandon weaker memory models in favor of implementing SC

Alpha, Sparc, PowerPC, ...
TSO, PSO, RMO, ...
RMO=WO?
SMP, DSM, CMP
Store is globally performed
Write-buffers
Implementing SC

1. The memory operations of each individual processor appear to all processors in the order the requests are made to the memory
   
   - Provided by cache coherence, which ensures that all processors observe the same order of loads and stores to an address

2. Any execution is the same as if the operations of all the processors were executed in some sequential order
   
   - Provided by enforcing a dependence between each memory operation and the following one
SC Data Dependence
SC Data Dependence

- **Stall**
  - Use in-order execution and blocking caches
  - Cache coherence plus allowing a processor to have only one request in flight at a time will provide SC
SC Data Dependence

- **Stall**
  - Use in-order execution and blocking caches
    - Cache coherence plus allowing a processor to have only one request in flight at a time will provide SC

- **Change architecture ⇒ Relaxed memory models**
  - Use OOO and non-blocking caches
    - Cache coherence and allowing multiple concurrent requests (to different addresses) gives high performance
    - Add fence operations to force ordering when needed
SC Data Dependence

• **Stall**
  - Use in-order execution and blocking caches
    • Cache coherence plus allowing a processor to have only one request in flight at a time will provide SC

• **Change architecture** ⇒ Relax memory models
  - Use OOO and non-blocking caches
    • Cache coherence and allowing multiple concurrent requests (to different addresses) gives high performance
    • Add fence operations to force ordering when needed

• **Speculate...**
Sequential Consistency Speculation

- Local load-store ordering uses standard OOO mechanism

- Globally non-speculative stores
  - Stores execute at commit -> stores are in-order!
Sequential Consistency Speculation

- Local load-store ordering uses standard OOO mechanism

- Globally non-speculative stores
  - Stores execute at commit -> stores are in-order!

- Globally speculative loads
  - **Guess** at issue that the memory location used by a load will not change between issue and commit of the instruction
    - this is equivalent to loads happening in-order at commit
  - **Check** at commit by remembering all loads addresses starting at issue and watching for writes to that location.

  - **Data Management** for rollback relies on the basic out-of-order speculative data management used for uni-processor rollback and instruction re-execution.
## SC Speculative Behavior

<table>
<thead>
<tr>
<th></th>
<th>CPU A</th>
<th>CPU B</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
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</tbody>
</table>

October 25, 2023  
MIT 6.5900 Fall 2023  
L14-25
SC Speculative Behavior

1: ST A

CPU A ----> CPU B
SC Speculative Behavior

1: ST A
2: LD A
SC Speculative Behavior

1: ST A
2: LD A

CPU A

CPU B
SC Speculative Behavior

1: ST A
2: LD A
3: LD A

CPU A

CPU B
SC Speculative Behavior

1: ST A
2: LD A
3: LD A

CPU A

CPU B
SC Speculative Behavior

1: ST A
2: LD A
3: LD A
4: ST A

CPU A
CPU B
SC Speculative Behavior

1: ST A
2: LD A
3: LD A
4: ST A

CPU A

CPU B

ST A
SC Speculative Behavior

1: ST A
2: LD A
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4: ST A

CPU A

CPU B

ST A
SC Speculative Behavior

1: ST A
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CPU A

CPU B
SC Speculative Behavior

1: ST A

2: LD A

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CPU A

CPU B

ST A

L14-25
SC Speculative Behavior

1: ST A
2: LD A
3: LD A
4: ST A

CPU A

CPU B

ST A
SC Speculative Behavior

1: ST A
2: LD A
3: LD A
4: ST A

CPU A

CPU B
Properly Synchronized Programs

• Very few programmers do programming that relies on SC; instead, they use higher-level synchronization primitives
  – locks, semaphores, monitors, atomic transactions
Properly Synchronized Programs

- Very few programmers do programming that relies on SC; instead, they use higher-level synchronization primitives
  - locks, semaphores, monitors, atomic transactions
- A “properly synchronized program” is one where each shared writable variable is protected (say, by a lock) so that there is no race in updating the variable
  - There is still race to get the lock
  - There is no way to check if a program is properly synchronized
- For properly synchronized programs, instruction reordering does not matter as long as updated values are committed before leaving a locked region
Release Consistency
[Garachorloo 1990]

- Only care about inter-processor memory ordering at thread synchronization points, not in between.
- Can treat all synchronization instructions as the only ordering points.

... Acquire(lock) // All following loads
    // get most recent written values

... Read and write shared data ..

Release(lock) // All preceding writes are globally visible
    // before lock is freed.
...

October 25, 2023
Takeaways

• SC is too low level a programming model. High-level programming should be based on critical sections & locks, atomic transactions, monitors, ...

• High-level parallel programming should be oblivious of memory model issues
  – Programmer should not be affected by changes in the memory model

• ISA definition for Load, Store, Memory Fence, synchronization instructions should
  – Be precise
  – Permit maximum flexibility in hardware implementation
  – Permit efficient implementation of high-level parallel constructs
Thank you!

Next Lecture:
On-Chip Networks