## Problem M8.1: Fetch Pipelines

Ben is designing a deeply-pipelined, single-issue, in-order MIPS processor. The first half of his pipeline is as follows:

| PC | PC Generation |
| :---: | :---: |
| F1 | ICache Access |
| F2 |  |
| D1 | Instruction Decode |
| D2 |  |
| RN | Rename/Reorder |
| RF | Register File Read |
| EX | Integer Execute |

There are no branch delay slots and currently there is no branch prediction hardware (instructions are fetched sequentially unless the PC is redirected by a later pipeline stage). Subroutine calls use JAL/JALR (jump and link). These instructions write the return address ( $\mathrm{PC}+4$ ) into the link register (r31). Subroutine returns use JR r31. Assume that PC Generation takes a whole cycle and that you cannot bypass anything into the end of the PC Generation phase.

## Problem M8.1.A

Pipelining Subroutine Returns
Immediately after what pipeline stage does the processor know that it is executing a subroutine return instruction? Immediately after what pipeline stage does the processor know the subroutine return address? How many pipeline bubbles are required when executing a subroutine return?

Louis Reasoner suggests adding a BTB to speed up subroutine returns. Why doesn't a standard BTB work well for predicting subroutine returns?

Instead of a BTB, Ben decides to add a return stack to his processor pipeline. This return stack records the return addresses of the $N$ most recent subroutine calls. This return stack takes no time to access (it is always presenting a return address).
Explain how this return stack can speed up subroutine returns. Describe when and in which pipeline stages return addresses are pushed on and popped off the stack.

## Problem M8.1.D

Return Stack Operation
Fill in the pipeline diagram below corresponding to the execution of the following code on the return stack machine:

A: JAL B
$A+1: A+2:$

B: JR r31
$B+1: \quad B+2$ :
...
Make sure to indicate the instruction that is being executed. The first two instructions are illustrated below. The crossed out stages indicate that the instruction was killed during those cycles.

| instruction |  |  |  |  | time |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| A | PC | F1 | F2 | D1 | D2 | RN | RF | EX |  |  |  |  |  |  |  |  |  |
| A+1 |  | PC | F1 | F2 | D1 | -2 | RN | RF | EX |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
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If the return address prediction is wrong, how is this detected? How does the processor recover, and how many cycles are lost (relative to a correct prediction)?

Problem M8.1.F
Further Improving Performance
Describe a hardware structure that Ben could add, in addition to the return stack, to improve the performance of return instructions so that there is usually only a one-cycle pipeline bubble when executing subroutine returns (assume that the structure takes a full cycle to access).

## Problem M8.2: Managing Out-of-order Execution

This problem investigates the operation of a superscalar processor with branch prediction, register renaming, and out-of-order execution. The processor holds all data values in a physical register file, and uses a rename table to map from architectural to physical register names. A free list is used to track which physical registers are available for use. A reorder buffer (ROB) contains the bookkeeping information for managing the out-of-order execution (but, it does not contain any register data values).

When a branch instruction is encountered, the processor predicts the outcome and takes a snapshot of the rename table. If a misprediction is detected when the branch instruction later executes, the processor recovers by flushing the incorrect instructions from the ROB, rolling back the "next available" pointer, updating the free list, and restoring the earlier rename table snapshot.

We will investigate the execution of the following code sequence (assume that there is no branch-delay slot):

```
loop: lw r1, 0(r2) # load r1 from address in r2
    addi r2, r2, 4 # increment r2 pointer
    beqz r1, skip # branch to "skip" if r1 is 0
    addi r3, r3, 1 # increment r3
skip: bne r2, r4, loop # loop until r2 equals r4
```

The diagram for Question M3.5.A on the next page shows the state of the processor during the execution of the given code sequence. An instance of each instruction in the loop has been issued into the ROB (the beqz instruction has been predicted not-taken), but none of the instructions have begun execution. In the diagram, old values which are no longer valid are shown in the following format: The rename table snapshots and other bookkeeping information for branch misprediction recovery are not shown.

Assume that the following events occur in order (though not necessarily in a single cycle):
Step 1. The first three instructions from the next loop iteration (lw, addi, beqz) are written into the ROB (note that the bne instruction has been predicted taken).
Step 2. All instructions which are ready after Step 1 execute, write their result to the physical register file, and update the ROB. Note that this step only occurs once.
Step 3. As many instructions as possible commit.
Update the diagram below to reflect the processor state after these events have occurred. Cross out any entries which are no longer valid. Note that the "ex" field should be marked when an instruction executes, and the "use" field should be cleared when it commits. Be sure to update the "next to commit" and "next available" pointers. If the load executes, assume that the data value it retrieves is $\mathbf{0}$.


Free List


Reorder Buffer (ROB)

|  | use | ex | op | p1 | PR1 | p2 | PR2 | Rd | LPRd | PRd |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| next to commit | X |  | Iw | p | P2 |  |  | r1 | P1 | P4 |
|  | X |  | addi | p | P2 |  |  | r2 | P2 | P5 |
|  | X |  | beqz |  | P4 |  |  |  |  |  |
|  | X |  | addi | p | P3 |  |  | r3 | P3 | P6 |
| next available | X |  | bne |  | P5 | p | P0 |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |
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## Problem M8.2.B

Assume that after the events from Question M3.6.A have occurred, the following events occur in order:

Step 1. The processor detects that the beqz instruction has mispredicted the branch outcome, and recovery action is taken to repair the processor state.
Step 2. The beqz instruction commits.
Step 3. The correct next instruction is fetched and is written into the ROB.
Fill in the diagram below to reflect the processor state after these events have occurred. Although you are not given the rename table snapshot, you should be able to deduce the necessary information from the diagram from Question M3.6.A. You do not need to show invalid entries in the diagram, but be sure to fill in all the fields which have valid data, and update the "next to commit" and "next available" pointers. Also make sure that the free list contains all available registers.


Free List

| $\square$ |
| :---: |
| $\square$ |
|  |
|  |
|  |
|  |
| $\vdots$ |

Reorder Buffer (ROB)


## Problem M8.2.C

Consider (1) a single-issue, in-order processor with no branch prediction and (2) a multipleissue, out-of-order processor with branch prediction. Assume that both processors have the same clock frequency. Consider how fast the given loop executes on each processor, assuming that it executes for many iterations.

Under what conditions, if any, might the loop execute at a faster rate on the in-order processor compared to the out-of-order processor?

Under what conditions, if any, might the loop execute at a faster rate on the out-of-order processor compared to the in-order processor?

## Problem M8.3: Exceptions and Register Renaming

Ben Bitdiddle has decided to start Bentel Corporation, a company specializing in high-end x86 processors to compete with Intel. His latest project is the Bentium 4, a superscalar, out-of-order processor with register renaming and speculative execution.

The Bentium 4 has 8 architectural registers (EAX, EBX, ECX, EDX, ESP, EBP, EDI, and ESI). In addition, the processor provides 8 internal registers T0-T7 not visible to the ISA that can be used to hold intermediary values used by micro-operations ( $\mu \mathrm{ops}$ ) generated by the microcode engine. The microcode engine is the decode unit and is used to generate $\mu$ ops for all the x86 instructions. For example, the following register-memory x86 instruction might be translated into the following RISC-like $\mu$ ops:

$$
\begin{aligned}
& \operatorname{ADD~R~} \mathrm{R}_{\mathrm{d}}, \mathrm{R}_{\mathrm{a}}, \operatorname{offset}\left(\mathrm{R}_{\mathrm{b}}\right) \rightarrow \quad \mathrm{LW} \quad \mathrm{~T} 0, \operatorname{offset}\left(\mathrm{R}_{\mathrm{b}}\right) \\
& \operatorname{ADD~} \mathrm{R}_{\mathrm{d}}, \mathrm{R}_{\mathrm{a}}, \mathrm{~T} 0
\end{aligned}
$$

All $16 \mu$ op-visible registers are renamed by the register allocation table (RAT) into a set of physical registers ( $\mathrm{P} 0-\mathrm{Pn}$ ). There is a separate shadow map structure that takes a snapshot of the RAT on a speculative branch in case of a misprediction. The block diagram for the front-end of the Bentium 4 is shown below:


For the Bentium 4, if an x86 instruction takes an exception before it is committed, the machine state is reset back to the precise state that existed right before the excepting instruction started executing. This instruction is then re-executed after the exception is handled. Ben proposes that the shadow map structure used for speculative branches can also be used to recover a precise state in the event of an exception. Specify a strategy that can be implemented for taking the least number of snapshots of the RAT that would still allow the Bentium 4 to implement precise exception handling.

Problem M8.3.B Minimizing Snapshots

Ben further states that the shadow map structure does not need to take a snapshot of all the registers in the Bentium 4 to be able to recover from an exception. Is Ben correct or not? If so, state which registers do not need to be recorded and explain why they are not necessary, or explain why all the registers are necessary in the snapshot.

Problem M8.3.C
Renaming Registers
Assume that the Bentium 4 has the same register renaming scheme as the Pentium 4. What is the minimum number of physical registers ( P ) that the Bentium 4 must have to allow register renaming to work? Explain your answer.

## Problem M8.4: Out-of-order Execution (Spring 2014 Quiz 2, Part C)

In this problem, we are going to update the state of the processor when different events happen. You are given an out-of-order processor in some initial state, as described by the registers (renaming table, physical registers, and free list), one-bit branch predictor, and re-order buffer. Your job is to show the changes that occur when some event occurs, starting from the same initial state except where noted. For partial credit, briefly describe what changes occur.

## Problem M8.4.A

Show the state of the processor if the first load completes (but does not commit).


| PHYS. REG. FILE |  |  | FREE LIST |  |
| :--- | :--- | :--- | :--- | :--- |
| P0 | (R1) | $p$ |  |  |
| P7 |  |  |  |  |
| P1 | (R2) | $p$ |  |  |
| P2 | (R3) | $p$ |  |  |
| P3 | (R4) | $p$ |  |  |
| P4 |  |  |  |  |
| P5 |  |  |  |  |
|  |  |  |  |  |
| P6 |  |  |  |  |
|  |  |  |  |  |
| P7 |  |  |  |  |


| $\xrightarrow{\text { Next to commit }}$ | RE-ORDER BUFFER (ROB) |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Use? | Ex | Op | P1 | PR1 | P2 | PR2 | Rd | LPRd | PRd |
|  | X |  | LD | p | P1 |  |  | R1 | PO | P4 |
| Next available | X |  | ADD |  | P4 | p | P3 | R3 | P2 | P5 |
|  | X |  | ADD |  | P4 | p | P1 | R2 | P1 | P6 |
|  | X |  | BGEZ | p | P3 |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |

## Problem M8.4.B

Show the state of the processor after the next instruction is issued.


| PHYS. REG. FILE |  |  | FREE LIST |
| :---: | :---: | :---: | :---: |
| PO | (R1) | p | P7 |
| P1 | (R2) | p |  |
| P2 | (R3) | p |  |
| P3 | (R4) | p |  |
| P4 |  |  |  |
| P5 |  |  |  |
| P6 |  |  |  |
| P7 |  |  |  |


| Next to commit | RE-ORDER BUFFER (ROB) |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Use? | Ex | Op | P1 | PR1 | P2 | PR2 | Rd | LPRd | PRd |
|  | X |  | LD | p | P1 |  |  | R1 | PO | P4 |
| Next available | X |  | ADD |  | P4 | p | P3 | R3 | P2 | P5 |
|  | x |  | ADD |  | P4 | p | P1 | R2 | P1 | P6 |
|  | X |  | BGEZ | p | P3 |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |

## Problem M8.4.C

From the state at the end of Question 2, as the next action can the processor issue (not execute) another instruction?

In one or two sentences, what does this say about our design? How can we improve it?

## Problem M8.4.D

Show the state of the processor if the first LD triggers a page fault and after abort finishes.

|  |  | REDICTOR |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 00 | 1 |  | S. RE |  | FREE LIST |
|  | 01 | 0 | PO | (R1) | p | P7 |
| 00: LD R1, 0 (R2) ミ | 10 | 1 | P1 | (R2) | p |  |
| 04: ADD R3, R1, R4 | 11 | 0 | P2 | (R3) | p |  |
| 0c: BGEZ R4, A |  | g TABLE | P3 | (R4) | p |  |
| $\begin{array}{ll\|l} \text { 10: LD R3, } 0(R 2) & \overline{\bar{O}} \\ \text { A: 14: SUB R1, R3, R2 } & \overline{\mathrm{Z}} \end{array}$ | R1 | P4 | P4 |  |  |  |
| 18: ADD R4, R3, R1 $\sim$ | R2 | P6 | P5 |  |  |  |
|  | R3 | P5 | P6 |  |  |  |
|  | R4 | P3 | P7 |  |  |  |


| Next to commit | RE-ORDER BUFFER (ROB) |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Use? | Ex | Op | P1 | PR1 | P2 | PR2 | Rd | LPRd | PRd |
|  | X |  | LD | p | P1 |  |  | R1 | PO | P4 |
| Next available | X |  | ADD |  | P4 | p | P3 | R3 | P2 | P5 |
|  | X |  | ADD |  | P4 | p | P1 | R2 | P1 | P6 |
|  | X |  | BGEZ | p | P3 |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |

## Problem M8.5 (Spring 2015 Quiz 2, Part B)

You are given an out-of-order processor that

- Issues at most one instruction per cycle
- Commits at most one instruction per cycle
- Uses an unified physical register file


## Problem M8.5.A

Consider the following code sequence:

| Addr |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| IO | (0x24) |  | Iw | r2, | (r4) | \# 0 |
| I1 | (0×28) |  | addi | r2, |  | \#16 |
| 12 | ( $0 \times 2 \mathrm{C}$ ) |  | lw | r3, | (r4) | \# 4 |
| I3 | (0x30) |  | blez | r3, | L1 |  |
| I4 | (0x34) |  | addi | r4, | r2, | \#8 |
| I5 | (0x38) |  | mul | r1, | r2, | -3 |
| I6 | (0x3C) |  | addi | r3, | r2, | \# 8 |
| I7 | ( $0 \times 40$ ) | L1: | add | r2, | r1, r3 | -3 |

Assume the branch instruction (blez) is not taken. Fill out the table below to identify all Read-AfterWrite (RAW), Write-After-Read (WAR), and Write-After-Write (WAW) dependencies in the above sequence.

Older Instruction

Younger Instruction

|  | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 10 | - |  |  |  |  |  |  |  |
| 11 | WAW RAW | - |  |  |  |  |  |  |
| 12 |  |  | - |  |  |  |  |  |
| 13 |  |  |  | - |  |  |  |  |
| 14 |  |  |  |  | - |  |  |  |
| 15 |  |  |  |  |  | - |  |  |
| 16 |  |  |  |  |  |  | - |  |
| 17 |  |  |  |  |  |  |  | - |

In Problems M8.5.B to M8.5.D, you should update the state of the processor when different events happen. The starting state in each question is the same, and the event specified in each question is the ONLY event that takes place for that question. The starting state is shown in the different structures: renaming table, physical registers, free list, two-bit branch predictor, global history buffer, and reorder buffer (ROB).

Note the following conventions:

- The valid bit for any entry is represented by " 1 ".
- The valid bit can be cleared by crossing it out.
- In the ROB, the "ex" field should be marked with " 1 " when an instruction starts execution, and the "use" field should be cleared when it commits. Be sure to update the "next to commit" and "next available" pointers, if necessary.
- Fill out the "after" fields in all the tables. Write new values in these boxes if the values change due to the event specified in the question. You do not have to repeat the values if they do not change due to the event.

In Questions 2 through 4, we will use the same code sequence as in Question 1:


The starting state of the processor is as follows:

- Instructions I0-I4 are already in the ROB.
- I0 (lw) has already finished execution.
- I1 (addi) and I2 (lw) have started executing but have not finished yet.
- I3 (blez) has been predicted to be Not-Taken by the branch predictor.
- I5 (mul) has completed the decode stage.
- I6 (addi) has completed the Fetch Stage.
- The next PC is set to $0 \times 40$, which is the PC of I7 (add).

Problem M8.5.B

The following figure shows the starting state of the processor. Suppose the decoded instruction I5 (mul) is now inserted into the ROB. Update the diagram to reflect the processor state after this event has occurred.

| Prediction Counter |  |  |
| :---: | :---: | :---: |
| Index | Before | After |
| $\mathbf{0 0 0}$ | 11 |  |
| $\mathbf{0 0 1}$ | 00 |  |
| $\mathbf{0 1 0}$ | 11 |  |
| $\mathbf{0 1 1}$ | 01 |  |
| $\mathbf{1 0 0}$ | 10 |  |
| $\mathbf{1 0 1}$ | 11 |  |
| $\mathbf{1 1 0}$ | 01 |  |
| $\mathbf{1 1 1}$ | 00 |  |



| Rename Table (Latest) |  |  |
| :---: | :---: | :---: |
| Name | Before | After |
| R1 | P0 |  |
| R2 | P5 |  |
| R3 | P6 |  |
| R4 | P7 |  |


| Rename Table <br> (Snapshot 1) |  | Valid |
| :---: | :---: | :---: |
|  | 1 |  |
| Name | Before | After |
| R1 | P0 |  |
| R2 | P5 |  |
| R3 | P6 |  |
| R4 | P3 |  |


| Physical Registers |  |  |
| :---: | :---: | :---: |
| Name | Value | Valid |
| P0 | 45 | 1 |
| P1 | 2 | 1 |
| P2 | -3 | 1 |
| P3 | 100 | 1 |
| P4 | 20 | 1 |
| P5 |  |  |
| P6 |  |  |
| P7 |  |  |
| P8 |  |  |
| P9 |  |  |
| P10 |  |  |


| Free List |
| :---: |
| P8 |
| P9 |
| P10 |
|  |
|  |
|  |
|  |
|  |
|  |


| Reorder Buffer (ROB) |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| use | ex | op | p1 | PR1 | p2 | PR2 | Rd | LPRd | PRd |
| 1 | 1 | Iw | 1 | P3 |  |  | r2 | P1 | P4 |
| 1 | 1 | addi | 1 | P4 |  |  | r2 | P4 | P5 |
| 1 | 1 | Iw | 1 | P3 |  |  | r3 | P2 | P6 |
| 1 |  | blez |  | P6 |  |  |  |  |  |
| 1 |  | addi |  | P5 |  |  | r4 | P3 | P7 |
|  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |
| Next to <br> commit |  |  |  |  |  |  |  |  |  |

Start from the same processor state, shown below. Suppose now I1 (addi) has completed execution. Commit as many instructions as possible. Update the diagram to reflect the processor state after I1 execution completes and as many instructions as possible have committed. Again, assume no other events take place.

| Prediction Counter |  |  |
| :---: | :---: | :---: |
| Index | Before | After |
| $\mathbf{0 0 0}$ | 11 |  |
| $\mathbf{0 0 1}$ | 00 |  |
| $\mathbf{0 1 0}$ | 11 |  |
| $\mathbf{0 1 1}$ | 01 |  |
| $\mathbf{1 0 0}$ | 10 |  |
| $\mathbf{1 0 1}$ | 11 |  |
| $\mathbf{1 1 0}$ | 01 |  |
| $\mathbf{1 1 1}$ | 00 |  |



| Next PC to be fetched |  |
| :---: | :---: |
| Before | After |
| $0 \times 40$ |  |


| Rename Table (Latest) |  |  |
| :---: | :---: | :---: |
| Name | Before | After |
| R1 | P0 |  |
| R2 | P5 |  |
| R3 | P6 |  |
| R4 | P7 |  |


| Rename Table <br> (Snapshot 1) |  | Valid |
| :---: | :---: | :---: |
|  | 1 |  |
| Name | Before | After |
| R1 | P0 |  |
| R2 | P5 |  |
| R3 | P6 |  |
| R4 | P3 |  |


| Physical Registers |  |  |
| :---: | :---: | :---: |
| Name | Value | Valid |
| P0 | 45 | 1 |
| P1 | 2 | 1 |
| P2 | -3 | 1 |
| P3 | 100 | 1 |
| P4 | 20 | 1 |
| P5 |  |  |
| P6 |  |  |
| P7 |  |  |
| P8 |  |  |
| P9 |  |  |
| P10 |  |  |


| Free List |
| :---: |
| P8 |
| P9 |
| P10 |
|  |
|  |
|  |
|  |
|  |
|  |


| Reorder Buffer (ROB) |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| use | ex | op | p1 | PR1 | p2 | PR2 | Rd | LPRd | PRd |
| 1 | 1 | Iw | 1 | P3 |  |  | r2 | P1 | P4 |
| 1 | 1 | addi | 1 | P4 |  |  | r2 | P4 | P5 |
| 1 | 1 | Iw | 1 | P3 |  |  | r3 | P2 | P6 |
| 1 |  | blez |  | P6 |  |  |  |  |  |
| 1 |  | addi |  | P5 |  |  | r4 | P3 | P7 |
|  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |
| Next to <br> commit |  |  |  |  |  |  |  |  |  |

Start from the same processor state, shown below. Suppose instruction I2 (lw) triggers an ALU overflow exception. Restore the architectural and microarchitectural state to recover from misspeculation. The exception handler for the processor is at address 0x8C (control is transferred to the exception handler after recovery). You do not need to worry about the number of cycles taken by recovery. Show the processor state after recovery.

| Prediction Counter |  |  |
| :---: | :---: | :---: |
| Index | Before | After |
| $\mathbf{0 0 0}$ | 11 |  |
| $\mathbf{0 0 1}$ | 00 |  |
| $\mathbf{0 1 0}$ | 11 |  |
| $\mathbf{0 1 1}$ | 01 |  |
| $\mathbf{1 0 0}$ | 10 |  |
| $\mathbf{1 0 1}$ | 11 |  |
| $\mathbf{1 1 0}$ | 01 |  |
| $\mathbf{1 1 1}$ | 00 |  |



| Rename Table (Latest) |  |  |
| :---: | :---: | :---: |
| Name | Before | After |
| R1 | P0 |  |
| R2 | P5 |  |
| R3 | P6 |  |
| R4 | P7 |  |


| Rename Table <br> (Snapshot 1) |  | Valid |
| :---: | :---: | :---: |
| Name | Before | After |
| R1 | P0 |  |
| R2 | P5 |  |
| R3 | P6 |  |
| R4 | P3 |  |


| Physical Registers |  |  |
| :---: | :---: | :---: |
| Name | Value | Valid |
| P0 | 45 | 1 |
| P1 | 2 | 1 |
| P2 | -3 | 1 |
| P3 | 100 | 1 |
| P4 | 20 | 1 |
| P5 |  |  |
| P6 |  |  |
| P7 |  |  |
| P8 |  |  |
| P9 |  |  |
| P10 |  |  |


| Free List |
| :---: |
| P8 |
| P9 |
| P10 |
|  |
|  |
|  |
|  |
|  |
|  |


| Reorder Buffer (ROB) |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| use | ex | op | p1 | PR1 | p2 | PR2 | Rd | LPRd | PRd |
| 1 | 1 | Iw | 1 | P3 |  |  | r2 | P1 | P4 |
| 1 | 1 | addi | 1 | P4 |  |  | r2 | P4 | P5 |
| 1 | 1 | Iw | 1 | P3 |  |  | r3 | P2 | P6 |
| 1 |  | blez |  | P6 |  |  |  |  |  |
| 1 |  | addi |  | P5 |  |  | r4 | P3 | P7 |
|  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |
| Next to <br> commit |  |  |  |  |  |  |  |  |  |

## Problem M8.6: Out-of-order Processor Design (Spring 2014 Quiz 2, Part D)



You are designing an out-of-order processor similar to the IBM 360/91 Tomasulo design shown above. This design distributes the re-order buffer around the processor, placing entries near their associated functional units. In such a design, the distributed ROB entries are called "reservation stations". Entries are allocated when the instruction is decoded and freed when the instruction is dispatched to the functional unit.

Your design achieves an average throughput of 1.5 instructions per cycle. Two-thirds of instructions are adds, and one-third are multiplies. The latency of each instruction type from allocation to completion is 5 cycles for adds and 14 cycles for multiplies.

| Type of operation | Fraction of instructions | Average latency |
| :--- | :--- | :--- |
| Add | $2 / 3$ | 5 |
| Multiply | $1 / 3$ | 14 |

The adder and multiplier are each fully pipelined with full bypassing. Once an instruction is dispatched to the $F U$, the adder takes 2 cycles and the multiplier takes 5 cycles.

| Throughput | Add latency | Multiply latency |
| :--- | :--- | :--- |
| 1.5 | 2 | 5 |

## Problem M8.6.A

How many entries are in use, on average, in the reservation station at each functional unit (adder, multiplier) in the steady state? Assume there are infinite entries available if needed. What is the average latency of an instruction in this machine? For partial credit, feel free to give any formulae you believe may be important to answer this question.

