# Computer System Architecture <br> 6.823 Quiz \#2 <br> April 7th, 2017 <br> Professors Daniel Sanchez and Joel Emer 

Name: $\qquad$
This is a closed book, closed notes exam. 85 Minutes

## 13 Pages (+2 Scratch)

Notes:

- Not all questions are of equal difficulty, so look over the entire exam and budget your time carefully.
- Please carefully state any assumptions you make.
- Show your work to receive full credit.
- Please write your name on every page in the quiz.
- You must not discuss a quiz's contents with other students who have not yet taken the quiz.
- Pages 14 and 15 are scratch pages. Use them if you need more space to answer one of the questions, or for rough work.

| Part A | $\square$ | 25 Points |
| :--- | :--- | :--- |
| Part B | $\square$ | 30 Points |
| Part C | $\square$ | 20 Points |
| Part D | $\square$ | 25 Points |

## Part A: Complex Pipelining ( 25 points)

Consider the following MIPS instruction sequence. An equivalent sequence of C-like pseudocode is also provided. F1, F2, and F3 are floating point registers.

I1: L.D
F2, $\theta(R 2)$
; F2 = *r2;
I2: L.D
F1, 0(R1)
; $\mathrm{F} 1={ }^{*} \mathrm{r}$;
I3: L.D
F2, 4(R1)
I4: MUL.D
F3, F1, F2
; $\mathrm{F} 2={ }^{*}(\mathrm{r} 1+4)$;

I5: ADD.D
F1, F2, F2
; F3 = F1 x F2;
I6: S.D
F3, 0(R2)
; F1 = F2 + F2;
I7: S.D
F1, 4(R1)
; *r2 = F3;
; ${ }^{*}(r 1+4)=F 1$;

## Question 1 (4 points)

Fill out the table below to identify all Read-After-Write (RAW), Write-After-Read (WAR), and Write-After-Write (WAW) dependencies in the above sequence. Do not worry about memory dependencies for this question. The dependency between I3 and I4 is already filled in for you.

Earlier (Older) Instructions

|  | I1 | I2 | I3 | I4 | I5 | I6 | I7 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| I1 | - |  |  |  |  |  |  |
| I2 |  | - |  |  |  |  |  |
| I3 |  |  | - |  |  |  |  |
| I4 |  |  | RAW | - |  |  |  |
| I6 |  |  |  |  | - |  |  |
| I7 |  |  |  |  |  | - |  |

## Question 2 (9 Points)

Calculate the number of cycles this code sequence would take to execute from issue of I1 to the issue of I7, inclusive, on a single-issue in-order pipelined machine. The machine uses a scoreboard and has no bypassing (as in Lecture 8). The floating point multiplier, adder, and load/store units are fully pipelined, so issue is never stalled by a busy functional unit (FU). The FUs latch their inputs. Assume that functional units have latencies as shown in the table below. Register write-back takes one additional cycle. Ignore write-back conflicts. I1 misses, but all other memory operations hit.

\section*{Operation Load/Store that hits Load/Store that misses Multiplies Adds <br> | Latency | 2 cycles | 6 cycles | 4 cycles 2 cycles |
| :--- | :--- | :--- | :--- |}

You may fill out the timing chart below to help you find the answer. Filling out the chart can give you partial credit. It is initialized for you below with the issue and completion/write-back cycles of II.

| Cycle | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Instruction <br> issue or <br> writeback | I |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |


| Cycle | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 | 31 | 32 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Instruction <br> issue or <br> writeback |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

$\qquad$

## Question 3 (12 Points)

Manually rename registers in the code sequence to eliminate all WAR and WAW dependences, and reorder the instructions in the code sequence to minimize execution time. You may use register names from F1 to F7. Show the new instruction sequence and give the number of cycles this sequence takes to execute on the scoreboarded in-order pipeline. Partial credit will be given for solutions with improved, but sub-optimal timing.

## Original instruction sequence Register-renamed and reordered sequence



You may fill out the timing chart below to help you find the answer, and for partial credit.

| Cycle | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Instruction <br> issue or <br> writeback |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

$\qquad$

## Part B: Out-of-Order Processing (30 points)

This question uses the out-of-order Data-in-ROB machine described in the Quiz 2 Handout. We describe events that affect the initial state shown in the handout. Label each event with one of the actions listed in the handout. If you pick a label with a blank ( $\qquad$ ), you also have to fill in the blank using the choices (i-v) listed below. If you pick "R. Illegal action", state why it is an illegal action. If in doubt, state your assumptions.

Example: Assume T11 data becomes available. Instruction I12 is issued and its effective address matches load buffer entry 4. Answer: (L, iv): Check the correctness of a speculation on memory address and find an incorrect speculation. (You can simply write L, iv)
a) Instruction I8 finishes execution and replaces T10's src1 tag with data, and sets the p1 bit.
b) Instruction I8 finishes execution and writes back the new value of R4 to T8's dest data field, and sets its pd bit.
c) Instruction I17 is dispatched to ROB entry T17. The instruction will write register R6, so tag T 17 is written into the R6 entry of the rename table, and the valid bit is set.
d) Instruction I 17 is dispatched to ROB entry T17. The instruction's first operand is register R3, so value 3980 is copied from the register file into T17's src1 field, and the p1 bit is set.
e) Instruction I18 has no entry in the BTB, so PC 0 xc 0 is fetched for I19.
f) Assume T11 data becomes available and the processor's divider unit is unpipelined (i.e. it can work on only one instruction at a time). Instruction I13 is not issued until the divide finishes.
g) Assume all instructions through I6 have committed. I7 commits and writes 4000 into the R2 entry of the register file.
h) Assume all instructions through I7 have committed. I8 commits and replaces T10's src1 tag with a data value and sets T10's p1 bit.
i) Assume T13 data becomes available, I14 is issued, and the branch is found to be predicted correctly as not taken. The relevant branch prediction counter is decremented (unless it is already 0 ).
j) Assume instruction I11 encodes an address offset of 4 (not shown in the figure). I11 is issued, writes address 4004 into entry 3 of the load buffer, sets the corresponding valid bit, and loads data from the cache.

## Part C: Multithreading (20 points)

In this problem you will evaluate the throughput improvement of multithreading on the following code, which computes the per-element product of two arrays:

```
float A[1024], B[1024], P[1024];
..
for (int i = 0; i < 1024; i++)
    P[i] = A[i] * B[i];
```

Here is the corresponding MIPS assembly code:

```
;; Assume:
;; R1 holds address of A[i]; initialized to base address of A
;; 4096(R1) holds address of B[i], based on offset from A[i]
;; 8192(R1) holds address of P[i], based on offset from A[i]
;; R2 holds number of iterations remaining; initialized to N
```

I1: loop: lw.s F1, 0(R1)
I2: lw.s F2, 4096(R1)
I3: mul.sF3, F1, F2
I4: $\quad$ sw.s F3, 8192(R1)
I5: addi R1, R1, 4
I6: addi R2, R2, -1
I7: bnez R2, loop
You run this code on a single-issue in-order processor. Assume the following:

- The processor can fetch and issue one instruction per cycle.
- If an instruction cannot be issued due to a data dependency, the processor stalls.
- Loads/stores take $\mathbf{4}$ cycles (i.e., if instruction I1 starts execution at cycle N, then instructions that depend on the result of I1 can only start execution at or after cycle $N+4$ ); multiplies take 3 cycles; and all other instructions execute in 1 cycle.
- The load/store unit and multiplier are fully pipelined (i.e., can start a new request each cycle).
- The end-of-loop branch is always predicted correctly.


## Question 1 (5 Points)

Suppose the code runs on a multithreaded processor that performs fixed switching: the processor switches to the next thread every cycle (round-robin), and if the instruction of the next thread is not ready, it inserts a bubble into the pipeline. What is the minimum number of threads required to fully utilize the processor every cycle while running this code? Explain.

## Question 2 (5 Points)

Now suppose the multithreaded processor performs data-dependent switching: the processor only switches to another thread when an instruction cannot execute due to a data dependence. If no threads have a ready instruction, the processor inserts a bubble into the pipeline. What is the minimum number of threads required to fully utilize the processor every cycle while running this code? Explain.

## Question 3 (10 Points)

Assume the fixed-switching policy of Question 1. Reorder and edit the sequence of instructions to minimize the number of threads that fully utilize the multithreaded pipeline. How many threads do you need? Explain.

Partial credit will be given for solutions with a reduced, but sub-optimal number of threads.
Original instruction sequence Write a reordered and edited sequence

```
loop: lw.s F1, 0(R1)
    lw.s F2, 4096(R1)
    mul.s F3, F1, F2
    sw.s F3, 8192(R1)
    addi R1, R1, 4
    addi R2, R2, -1
    bnez R2, loop
```

Number of threads needed to fill the pipeline with reordered code: $\qquad$

## Part D: Centralized vs. Decentralized Issue ( 25 points)



This problem focuses on the issue logic of a superscalar out-of-order machine. You will explore the tradeoffs between a centralized issue buffer (left) and decentralized reservation stations (right). In both designs, an issue buffer entry is allocated when each instruction is decoded and is freed when the instruction is dispatched to a functional unit. The decentralized design (right), introduced by Tomasulo in the IBM 360/91, distributes the issue buffer entries around the processor, with one set of entries per functional unit. In such a design, the distributed entries are called "reservation stations". Do not worry about instruction commit or speculative buffering; you will focus on stages from entry allocation to instruction dispatch and completion.

The following applies to both designs. Your desired average throughput is 1.5 instructions per cycle. Consider a stream of floating point instructions that consists of $2 / 3$ adds and $1 / 3$ multiplies. For this stream, you observe that the average latency of an instruction from allocation in issue buffer to functional unit completion is 12 cycles. The processor's adder and multiplier are each fully pipelined. Once an instruction is dispatched to the functional unit, both the adder and multiplier take 3 cycles.

| Type of operation | Stream instruction ratio | FU latency |
| :--- | :--- | :--- |
| Add | $2 / 3$ | 3 cycles |
| Multiply | $1 / 3$ | 3 cycles |


| Average throughput | Average total latency |
| :--- | :--- |
| 1.5 instructions per cycle | 12 cycles |

## Question 1 (8 points)

Consider the centralized issue buffer. In steady state, how many issue buffer entries are in use on average?

## Question 2 (9 points)

Now consider the decentralized design. You observe that the average latency of add instructions from allocation to completion is 14 cycles for the stream of interest. How many reservation station entries are in use, on average, at each functional unit (adder, multiplier) in steady state?

| Average Adder reservation station entries |  |
| ---: | :--- |
| Average Multiplier reservation station entries |  |

## Question 3 (4 points)

Again consider the decentralized design. Suppose we run an instruction stream symmetric to the original. It is comprised of $1 / 3$ adds and $2 / 3$ multiplies, and the average latency of multiply instructions from allocation to functional unit completion is 14 cycles. How many reservation station entries are in use, on average, at each functional unit (adder, multiplier) in steady state? For full and/or partial credit, explain your reasoning.

| Average Adder reservation station entries |  |
| ---: | :--- |
| Average Multiplier reservation station entries |  |

## Question 4 (4 points)

Qualitatively, name one advantage and one disadvantage of the distributed reservation station design over the centralized issue buffer. Explain.

## Scratch Space

Use these extra pages if you run out of space or for your own personal notes. We will not grade this unless you tell us explicitly in the earlier pages.

