

### Contributors to the course material

- Arvind, Rishiyur S. Nikhil, Joel Emer, Muralidaran Vijayaraghavan
- Staff and students in 6.375 (Spring 2013),
   6.S195 (Fall 2012), 6.S078 (Spring 2012)
  - Asif Khan, Richard Ruhler, Sang Woo Jun, Abhinav Agarwal, Myron King, Kermin Fleming, Ming Liu, Li-Shiuan Peh
- External
  - Prof Amey Karkare & students at IIT Kanpur
  - Prof Jihong Kim & students at Seoul Nation University
  - Prof Derek Chiou, University of Texas at Austin
  - Prof Yoav Etsion & students at Technion

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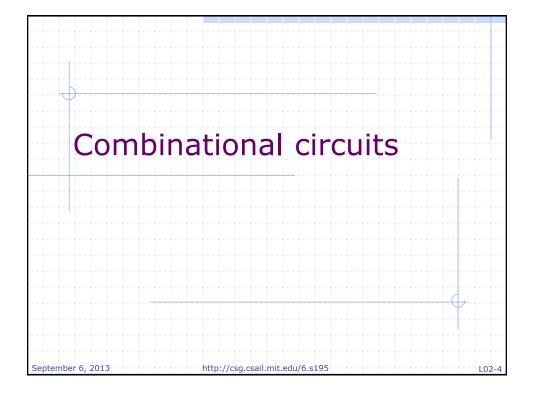
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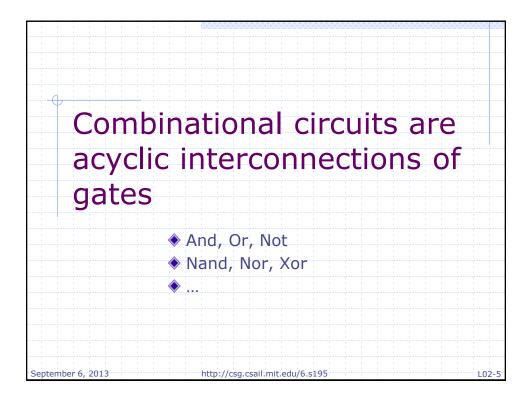
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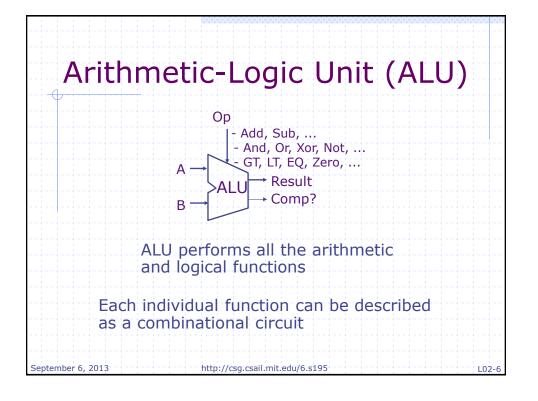
# Content Design of a combinational ALU starting with primitive gates And, Or and Not Combinational circuits as acyclic wiring diagrams of primitive gates Introduction to BSV

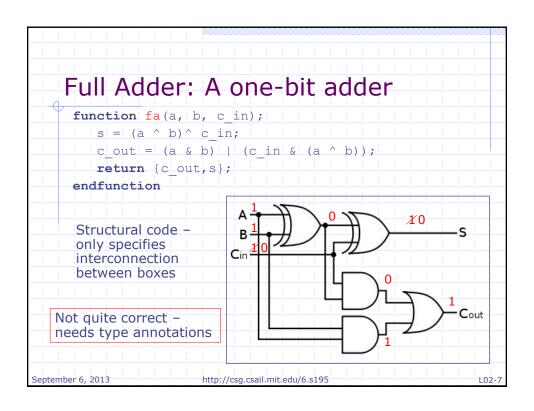
- Intro to types enum, typedefs, numeric types, int#(32) vs integer, bool vs bit#(1), vectors
- Simple operations: concatenation, conditionals, loops
- Functions
- Static elaboration and a structural interpretation of the textual code

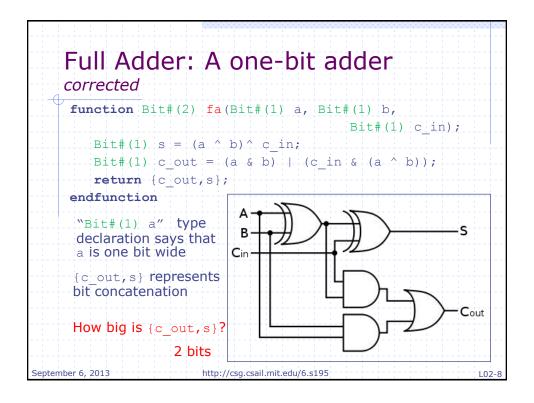
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# Types A type is a grouping of values: Integer: 1, 2, 3, ... Bool: True, False Bit: 0,1 A pair of Integers: Tuple2# (Integer, Integer) A function fname from Integers to Integers: function Integer fname (Integer arg) Every expression and variable in a BSV program has a type; sometimes it is specified explicitly and sometimes it is deduced by the compiler Thus we say an expression has a type or belongs to a type The type of each expression is unique

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#### 

```
Type synonyms

typedef bit [7:0] Byte; The same

typedef Bit#(8) Byte;

typedef Bit#(32) Word;

typedef Tuple2#(a,a) Pair#(type a);

typedef Int#(n) MyInt#(type n); The same

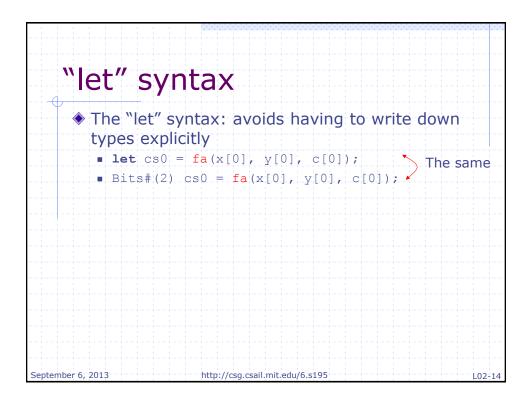
typedef Int#(n) MyInt#(numeric type n);
```

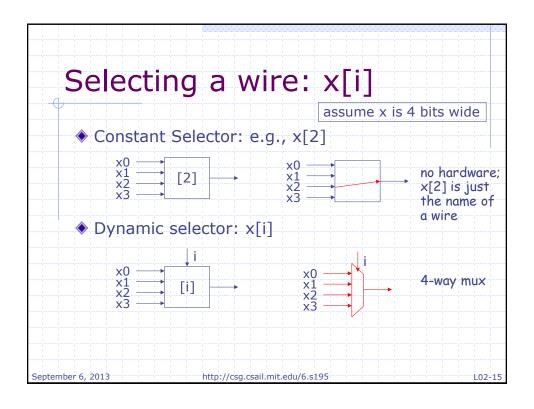
#### Type declaration versus deduction ◆ The programmer writes down types of some expressions in a program and the compiler deduces the types of the rest of expressions If the type deduction cannot be performed or the type declarations are inconsistent then the compiler complains **function** Bit#(2) **fa**(Bit#(1) a, Bit#(1) b, Bit#(1) c in); Bit # (1) s = (a ^ b) ^ c in; Bit#(2) c out = $(a \& b) + (c in \& (a \land b));$ return {c out,s}; type error endfunction Type checking prevents lots of silly mistakes

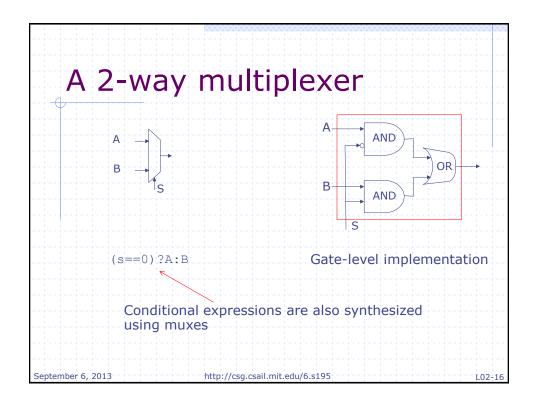
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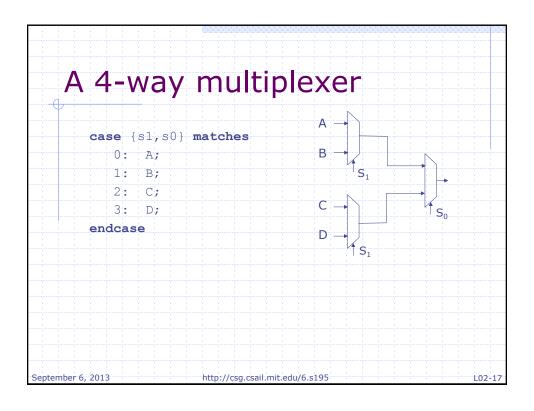
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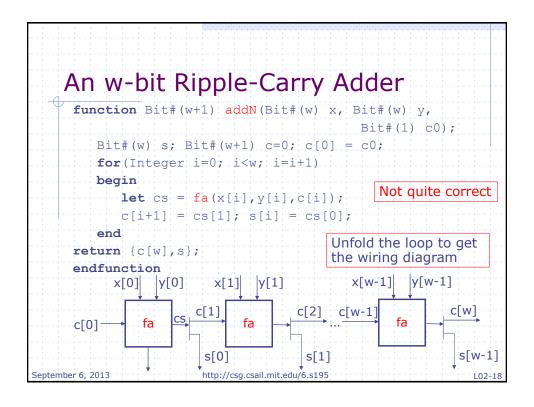
```
2-bit Ripple-Carry Adder
          x[0] | y[0] | x[1] | y[1]
                                      fa can be used as a
                                      black-box long as we
                  c[1]
     c[0]-
                               → c[2]
                                      understand its type
                                      signature
               s[0]
                         s[1]
    function Bit#(3) add(Bit#(2) x, Bit#(2) y,
                                             Bit#(1) c0);
       Bit#(2) s = 0; Bit#(3) c=0; c[0] = c0;
       let cs0 = fa(x[0], y[0], c[0]);
             c[1] = cs0[1]; s[0] = cs0[0];
       let cs1 = fa(x[1], y[1], c[1]);
            c[2] = cs1[1]; s[1] = cs1[0];
       return {c[2],s};
                              The "let" syntax avoids having
                               to write down types explicitly
    endfunction
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```











#### 

```
TAdd# (w, 1) Versus w+1

Sometimes we need to perform operations in the types world that are very similar to the operations in the value world

Examples: Add, Mul, Log

We define a few special operators in the types world for such operations

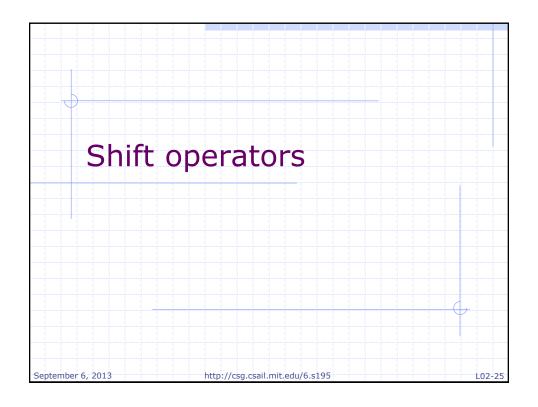
Examples: TAdd# (m, n), TMul# (m, n), ...
```

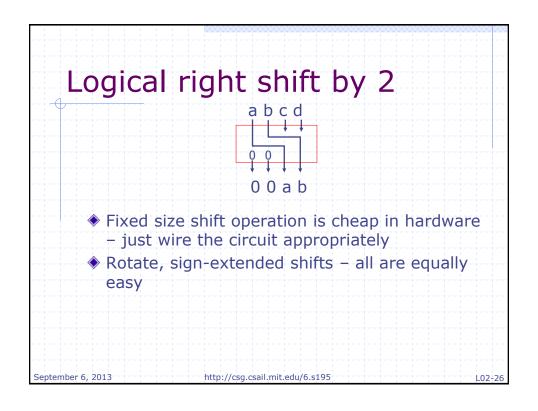
```
A w-bit Ripple-Carry Adder
    corrected
     function Bit # (TAdd# (w, 1))
                                  addN(Bit\#(w) x, Bit\#(w) y,
                                              Bit#(1) c0);
        Bit#(w) s; Bit#(TAdd#(w,1)) c; c[0] = c0;
        let valw \(\pi\) valueOf(w);
                                                 types world
        for(Integer i=0; i<valw; i=i+1)</pre>
                                                  equivalent of w+1
            let cs = fa(x[i],y[i],c[i]);
                                                  Lifting a type
            c[i+1] = cs[1]; s[i] = cs[0];
                                                  into the value
                                                  world
     return {c[valw],s};
     endfunction
           Structural interpretation of a loop – unfold it to
           generate an acyclic graph
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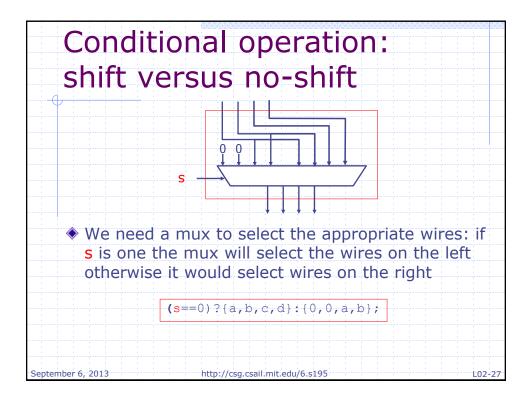
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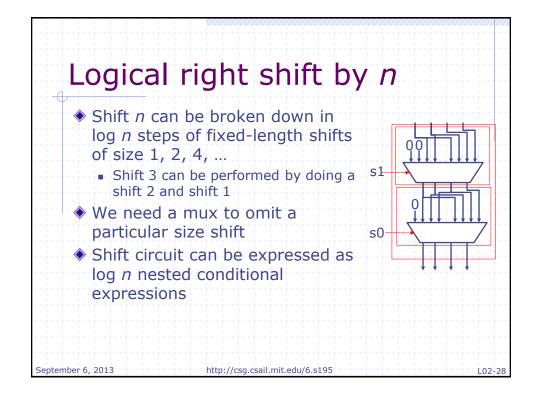
#### Integer versus Int#(32)

- In mathematics integers are unbounded but in computer systems integers always have a fixed size
- BSV allows us to express both types of integers, though unbounded integers are used only as a programming convenience

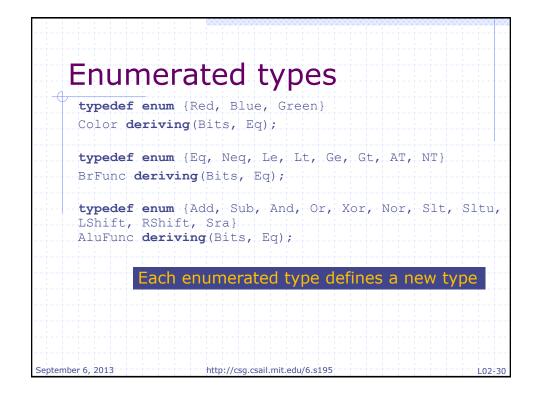






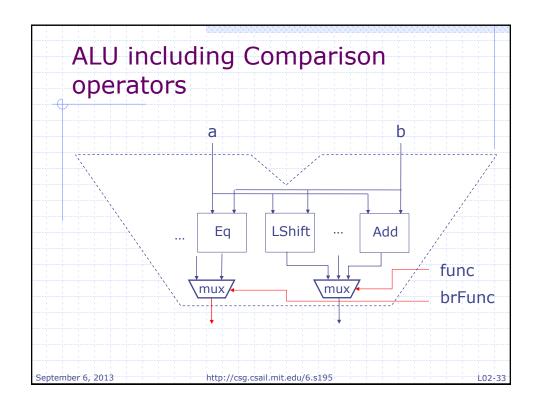


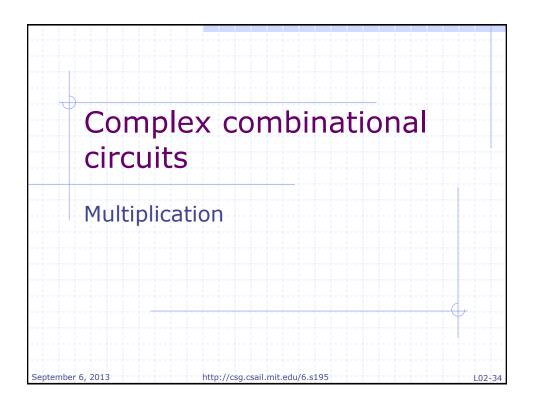
Α	digression on types
<del>+ + + + + + + + + + + + + + + + + + + </del>	Suppose we have a variable c whose values can represent three different colors
	<ul> <li>We can declare the type of c to be Bit#(2) and say that 00 represents Red, 01 Blue and 10 Green</li> </ul>
•	A better way is to create a new type called Color as follows:
	<pre>typedef enum {Red, Blue, Green} Color deriving(Bits, Eq);</pre>
Types progressive that represent color from bits	representation to the three colors and also provide a function to test if the two colors are equal. If you do
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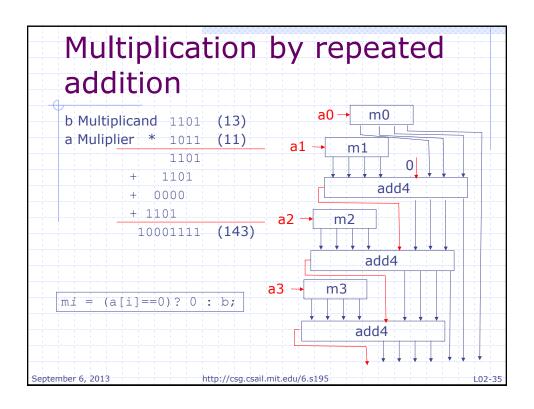


```
Combinational ALU
 function Data alu (Data a, Data b, AluFunc func);
   Data res = case(func)
                             Given an implementation of
      Add: (a + b);
                             the primitive operations like
      Sub: (a - b);
                             addN, Shift, etc. the ALU
      And : (a & b);
                             can be implemented simply
                             by introducing a mux
      Or : (a | b);
                             controlled by op to select the
      Xor : (a ^ b);
                             appropriate circuit
      Nor : ~ (a | b);
      Slt : zeroExtend( pack( signedLT(a, b) ) );
      Sltu : zeroExtend( pack( a < b ) );</pre>
      LShift: (a << b[4:0]);
      RShift: (a >> b[4:0]);
      Sra : signedShiftRight(a, b[4:0]);
   endcase;
   return res;
 endfunction
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```

```
Comparison operators
     function Bool aluBr (Data a, Data b, BrFunc brFunc);
        Bool brTaken = case (brFunc)
          Eq : (a == b);
          Neq: (a != b);
          Le : signedLE(a, 0);
          Lt : signedLT(a, 0);
          Ge : signedGE(a, 0);
          Gt : signedGT(a, 0);
          AT : True;
          NT : False;
        endcase;
        return brTaken;
      endfunction
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```







```
Combinational 32-bit multiply

function Bit#(64) mul32(Bit#(32) a, Bit#(32) b);
    Bit#(32) prod = 0;
    Bit#(32) tp = 0;

for(Integer i = 0; i < 32; i = i+1)
begin
    Bit#(32) m = (a[i]==0)? 0 : b;
    Bit#(33) sum = add32(m,tp,0);
    prod[i] = sum[0];
    tp = truncateLSB(sum);
end
    return {tp,prod};
endfunction</pre>
```

## Design issues with combinational multiply

- Lot of hardware
  - 32-bit multiply uses 31 add32 circuits
- Long chains of gates
  - 32-bit ripple carry adder has a 31-long chain of gates
  - 32-bit multiply has 31 ripple carry adders in sequence!

The speed of a combinational circuit is determined by its longest input-to-output path

Can we do better?

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