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## Overloading and Type classes

- Overloading: using a common name for similar, but conceptually distinct operations
- Example:
- $\mathrm{n} 1<\mathrm{n} 2 \quad$ where n 1 and n 2 are integers
- s1 < s2 where s1 and s2 are strings
- Distinct: These orderings may have nothing to do with each other -- their implementations are likely to be totally different
- Similar: integer " $<$ " and string " $<$ " may share some common properties, such as
- transitivity: $(\mathrm{a}<\mathrm{b})$ and $(\mathrm{b}<\mathrm{c}) \Rightarrow(\mathrm{a}<\mathrm{c})$
- irreflexivity: $(a<b) \Rightarrow \sim(b<a)$
- Type classes may be seen as a systematic mechanism for overloading


## Type classes

- A type class is a collection of types, all of which share a common set of operations with similar type signatures
- Examples:
- All types t in the "Eq" class have equality and inequality operations:

```
class Eq t where
    (==) :: t -> t -> Bool
    (/=) :: t -> t ->> Bool
```

- All types t and n in the "Bits" class have operations to convert objects of type $t$ into bit vectors of size n and back:
class Bits $t \mathrm{n}$ where
pack : : t $\rightarrow$ Bit $n$
unpack : : Bit $n \rightarrow t$
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## How does a type become a member of a class?

- Membership is not automatic: a type has to be declared to be an instance of a class, and implementations of the corresponding operations must be supplied
- Until $t$ is a member of Eq, you cannot use the "==" operation on values of type $t$
- Until t is a member of Bits, you cannot store them in hardware state elements like registers, memories and FIFOs
- The general way to do this is with an "instance" declaration
- A frequent shortcut is to use a "deriving" clause when declaring a type


## Class "Bits"

```
data Day = Sun | Mon | Tue | Wed | Thu | Fri | Sat
    deriving (Bits)
```


## The "deriving" clause

- Declares type Day to be an instance of the Bits class
- Defines the two associated functions

```
pack :: Day m Bit 3
unpack :: Bit 3 -> Day
```


## "deriving (Bits)" for algebraic types

```
data T = C0 ta tb | C1 tc | C2 td te tf
    deriving (Bits)
```

The canonical "pack" function created by "deriving (Bits)" produces the following packings:

where "tag" is 0 for $\mathrm{C} 0,1$ for C 1 , and 2 for C 2.

## "deriving (Bits)" for structs

- The canonical "pack" function simply bitconcatenates the packed versions of the fields:

```
struct PktHdr =
            node :: Bit 6 -- NodeID
            port :: Bit 5 -- PortID
            cos :: Bit 3 -- CoS
            dp :: Bit 2 -- DropPrecedence
            ecn :: Bool
            res :: Reserved 1
            length :: Bit 14 -- PacketLength
            crc :: Bit 32
    deriving (Bits)
```

                    Bit 6 Bit 5 Bit \(3 \quad\)..
    
## Explicit pack \& unpack

```
data T = A (Bit 3) | B (Bit 5) | Ptr (Bit 31)
    deriving (Bits)
```

- Explicit "instance" decls. may permit more efficient packing than 33 bits

instance Bits $T 32$ where
pack (A a3) $=0 b 00$ ++ (zeroExtend a3)
pack ( B b5) $=0 \mathrm{~b} 01++$ (zeroExtend b 5 )
pack (Ptr p31) = 0b1 ++ p31
unpack $x=$ if $x[31: 30]==0 b 00$ then $A \times[2: 0]$ elseif $x[31: 30]==0 b 01$ then $B \times[4: 0]$ elseif $x[31: 31]==0 b 1$ then Ptr $\times[30: 0]$ ? יhttyp://www.csg.[cs.mit.edu/IAPBlue


## Class "Eq"

$$
\begin{aligned}
& \text { class Eq } t \text { where } \\
& (==):: t \rightarrow t \rightarrow \text { Bool } \\
& (/=):: t \rightarrow t \rightarrow \text { Bool }
\end{aligned}
$$

- "deriving (Eq)" will generate the natural versions of these operators automatically
- Are the tags equal?
- And, if so, are the corresponding fields equal?
- An "instance" declaration may be used for other meanings of equality, e.g.,
- "two pointers are equal if their bottom 20 bits are equal"
- "two values are equal if they hash to the same address"


## Type "Integer" and class "Literal"

- The type "Integer" refers to pure, unbounded, mathematical integers
- and, hence, Integer is not in class Bits, which can only represent bounded quantities
- Integers are used only as compile time entities
- The class "Literal" contains a function:
class Literal $t$ where
fromInteger : : Integer $\rightarrow$ t


## Class "Literal"

- Types such as (Bit n), (Int n), (Uint $n$ ) are all members of class Literal
- Thus,
(fromInteger 523) : : Bit 13
represents the integer 523 as a 13 -bit quantity
- while
(fromInteger 523) : : Int 13
represents the integer 523 as a 13 -bit Int type
- This is how all literal numbers in the program text, such as "0" or "1", or "23", or "523" are treated, i.e., they use the systematic overloading mechanism to convert them to the desired type


## Type classes for numeric types

- More generally, type classes can be seen as constraints on types
- Examples:
- For all numeric types t1, t2, t3 in the "Add" class, the value of t 3 is the sum of the values of t 1 and t 2 .
- For all numeric types t1, t2 in the "Log" class, the value of t2 is large enough that a (Bit t2) value can represent values in the range 0 to valueOf t1-1
- These classes are used to represent/derive relationships between various "sizes" in a piece of hardware


## Type classes for numeric types

- Suppose we have an array of $n$ locations. An index into the array needs $\mathrm{k}=\log _{2}(\mathrm{n})$ bits to represent values in the range 0 to $n-1$

```
mkTable :: (Bits t ts, Log n k) => Table n t
mkTable =
    module
        a :: Array (Bit k) t
        a <- mkArrayFull
        index :: Reg (Bit k)
        index <- mkRegU
        ...
```


## Outline

- Type classes $\sqrt{ }$
- Class Eq
- Type Bit and Class Bits
- Type Integer and Class literal
- Type classes for numeric types
- Instruction Encoding $\Leftarrow$



## MIPS Instruction Formats:Load/Store

Load/Store Instructions

| 100000 | base | dest | signed offset | LB rt, offset(rs) <br> LH rt, offset(rs) |
| :--- | :--- | :--- | :--- | :--- |
| 100001 | base | dest | signed offset | LW rt, offset(rs) |
| 10001 | base | dest | signed offset | LBU rt, offset(rs) |
| 100100 | base | dest | signed offset | LHU rt, offset(rs) |
| 100101 | base | dest | signed offset | SB rt, offset(rs) |
| 101000 | base | dest | signed offset | SH rt, offset(rs) |
| 101001 | base | dest | signed offset | SW rt, offset(rs) |
| 101011 | base | dest | signed offset |  |



## MIPS Instruction Formats:

 Jumps/Branches| 000010 | target |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 000011 | target |  |  |  |  |
| 000000 | sre | 00000 | 00000 | 00000 | 001000 |
| 000000 | sre | 00000 | dest | 00000 | 001001 |
| 000100 | srcl | src2 | signed offset |  |  |
| 000101 | srcl | src2 | signed offset |  |  |
| 000110 | sre | 00000 | signed offset |  |  |
| 000111 | sre | 00000 | signed offset |  |  |
| 010100 | srcl | src2 | signed offset |  |  |
| 010101 | srcl | src2 | signed offset |  |  |
| 010110 | src | 00000 | signed offset |  |  |
| 010111 | sre | 00000 | signed offset |  |  |
| 000001 | src | 00000 | signed offset |  |  |
| 000001 | sre | 00001 | signed offset |  |  |
| 000001 | src | 00010 | signed offset |  |  |
| 000001 | sre | 00011 | signed offset |  |  |
| 000001 | src | 10000 | signed offset |  |  |
| 000001 | sre | 10001 | signed offset |  |  |
| 000001 | sre | 10010 | signed offset |  |  |
| 000001 | sre | 10011 | signed offset |  |  |

J target JAL target
JR rs
JALR rd, rs BEQ rs, rt, offset BNE rs, rt, offset BLEZ rs, offset BGTZ rs, offset BEQL rs, rt, offset BNEL rs, rt, offset BLEZL rs, offset BGTZL rs, offset BLTZ rs, offset BGEZ rs, offset BLTZL rs, offset BGEZL rs, offset BLTZAL rs, offset BGEZAL rs, offset BLTZALL rs, offset BGEZALL rs, offset

## Decoding MIPS Instructions

- The input instruction formats for decoding are fixed but we choose the output instruction formats depending upon our need.
- Dan' s decoded format
- Jacob's decoded format
- Instruction decoding can be expressed as pack/unpack of these defined types into 32-bit values that correspond to MIPS instructions


## Naming the fields in MIPS instructions

| opcode | $=\mathrm{b} 32[31: 26]$ |
| :--- | :--- |
| rs | $=\mathrm{b} 32[25: 21]$ |
| rt | $=\mathrm{b} 32[20: 16]$ |
| rd | $=\mathrm{b} 32[15: 11]$ |
| shiftamt | $=\mathrm{b} 32[10: 6]$ |
| funct | $=\mathrm{b} 32[5: 0]$ |
| imm | $=\mathrm{b} 32[15: 0]$ |
| itarget | $=\mathrm{b} 32[25: 0]$ |
| zr | $=0 b 000000$ |
| brt | $=b 32[20: 16]$ |

As a convenience we can define new data types to refer to the contents some fields

| opcode | $::$ OpcodeT |
| :--- | :--- |
| rs | $::$ RegT |
| rt | $::$ RegT |
| rd | $::$ RegT |
| funct | $::$ FunctionT |

## OpcodeT



## Dan's format

data MIPSInstructionT =
LW_T \{base::RegT; dest::RegT; soff::ImmT;\}
SW_T \{base::RegT; dest::RegT; soff::ImmT;\} |
ADDI_T \{src::RegT; dest::RegT; simm::ImmT;\} |
ADDIU_T \{src::RegT; dest::RegT; simm::ImmT;\} |
ADD_T \{src1::RegT; src2::RegT; dest::RegT;\} |
ADDU_T \{src1::RegT; src2::RegT; dest::RegT;\} |
J_T \{target: : JumpTargetT; \} |
JAL_T \{target::JumpTargetT; \} |
BEQ_T \{src1::RegT; src2::RegT; simm::ImmT; \}
BNE_T \{src1::RegT; src2::RegT; simm::ImmT;\} |
JR_T \{src: : RegT; \}
JALR_T \{src::RegT; dest::RegT; \} |

| type RegT $=$ Bit 5 |
| :--- | :--- |
| type ImmT $=$ Bit 16 |
| type JumpTargetT $=$ Bit 26 |

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## Dan's pack

```
instance Bits MIPSInstructionT 32 where
        pack (LW_T {base; dest; soff;}) =
        (pack LW) ++ (pack base) ++ (pack dest) ++ (pack soff)
    pack (SW_T {base; dest; soff;}) =
        (pack SW) ++ (pack base) ++ (pack dest) ++ (pack soff)
            ...
```


## Dan's unpack

```
instance Bits MIPSInstructionT 32 where
    unpack b32 =
        let
            opcode :: OpcodeT = unpack b32[31:26]
rs : : RegT \(=\) unpack b32[25:21]
            rt :: RegT = unpack b32[20:16]
            rd :: RegT = unpack b32[15:11]
            shiftamt = unpack b32[10:6]
            funct :: FunctionT = unpack b32[5:0]
            imm :: ImmT = unpack b32[15:0]
            itarget = unpack b32[25:0]
            zr = unpack 0b000000
            brt :: RegT = unpack b32[20:16]
        in
            case opcode of ...
```

unpack is like decoding the instruction

## Dan's unpack continued



## Jacob's format

```
data Instruction =
        Immediate op :: Op
        rs :: CPUReg
        rt :: CPUReg
        imm :: UInt16
    | Register rs :: CPUReg
        rt :: CPUReg
        rd :: CPUReg
        sa :: UInt5
        funct :: Funct
    RegImm rs :: CPUReg
        op :: REGIMM
        imm :: UInt16
    Jump op :: Op
        target :: UInt26
    Nop
```

Need to define crureg, UInt5, UInt16, UInt26, REGIMM, op and Funct

## CPUReg Type: mips Instructions

| data CPUReg = | Reg0 <br> Reg4 <br> Reg8 <br> Reg12 <br> Reg16 <br> Reg20 <br> Reg24 <br> Reg28 <br> de | Reg1 <br> Reg5 <br> Reg9 <br> Reg13 <br> Reg17 <br> Reg21 <br> Reg25 <br> Reg29 <br> ving | Reg2 <br> Reg6 <br> Reg10 <br> Reg14 <br> Reg18 <br> Reg22 <br> Reg26 <br> Reg30 <br> ts, Eq | Reg3 <br> Reg7 <br> Reg11 <br> Reg15 <br> Reg19 <br> Reg23 <br> Reg27 <br> Reg31 <br> Bounded) |
| :---: | :---: | :---: | :---: | :---: |

```
type UInt32 = Bit 32
type UInt26 = Bit 26
type UInt16 = Bit 16
type UInt5 = Bit 5
```


## Op Type: mips Instructions

```
data Op = SPECIAL | REGIMM
    J | JAL | BEQ | BNE | BLEZ | BGTZ
    ADDI | ADDIU | SLTI | SLTIU | ANDI | ORI | XORI | LUI
    COPO | COP1 | COP2 | OP19
    | BEQL | BNEL | BLEZL | BGTZL
    | DADDIe | DADDIUe | LDLe | LDRe
    | OP28 | OP29 | OP30 | OP31
    Lb | LH | LWL | LW | LbU | LHU | LWR | LWUe
    | SB | SH | SWL | SW | SDLe | SDRe | SWR | CACHEd
    | LL | LWC1 | LWC2 | OP51 | LLDe | LDC1 | LDC2 | LDe
    SC | SWC1 | SWC2 | OP59 | SCDe | SDC1 | SDC2 | SDe
    deriving (Eq, Bits)
```

| Funct TyPe: MIPS Instructions $\quad \begin{array}{r}\text { L5-30 } \\ \text { Arvind }\end{array}$ |
| :---: |
|  |

## Funct Type: mIPS Instructions

```
data REGIMM = BLTZ | BGEZ | BLTZL | BGEZL
            | R4 | R5 | R6 | R7
            TGEI | TGEIU | TLTI | TLTIU
            TEQI | R13 | TNEI | R15
            | BLTZAL | BGEZAL | BLTZALL | BGEZALL
            | R20 | R21 | R22 | R23
```



```
            | R28 | R29 | R30 | R31
    deriving (Bits,Eq)
```


## Instruction Decode- Pack

```
instance Bits Instruction }32\mathrm{ where
    pack :: Instruction -> Bit 32
    pack (Immediate op rs rt imm) =
        (pack op) ++ (pack rs) ++ (pack rt) ++ (pack imm)
    pack (Register rs rt rd sa funct) =
            (pack SPECIAL) ++ (pack rs) ++ (pack rt) ++
                (pack rd) ++ (pack sa) ++ (pack funct)
    pack (RegImm rs op imm) =
            (pack REGIMM) ++ (pack rs) ++ (pack op) ++
                (pack imm)
    pack (Jump op target) = (pack op) ++ (pack target)
    pack (Nop) = 0
```



## Instruction Decode - Unpack

```
instance Bits Instruction 32 where
    unpack :: Bit 32 -> Instruction
    unpack bs when isImmInstr bs = Immediate {
        op = unpack bs[31:26];
        rs = unpack bs[25:21];
        rt = unpack bs[20:16];
        imm = unpack bs[15:0]; }
    unpack bs when isREGIMMInstr bs = RegImm {
        rs = unpack bs[25:21];
        op = unpack bs[20:16];
        imm = unpack bs[15:0]; }
```

    unpack bs when isJumpInstr bs = Jump \(\{\)
        op = unpack bs[31:26];
        target \(=\) unpack bs[25:0];\}
    
## Decoding Functions

```
isREGIMMInstr : : Bit (SizeOf Instruction) -> Bool
isREGIMMInstr bs = bs[31:26] == (1::Bit 6)
isJumpInstr :: Bit (SizeOf Instruction) -> Bool
isJumpInstr bs = isJumpOp (unpack bs[31:26])
isSpecialInstr :: Bit (SizeOf Instruction) -> Bool
isSpecialInstr bs = bs[31:26] == (0::Bit 6)
isImmInstr :: Bit (SizeOf Instruction) -> Bool
isImmInstr bs = not (isSpecialInstr bs || isREGIMMInstr bs
                    || isJumpInstr bs )
```

