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December 30, 2013

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_01-2

Content

- Design of a combinational ALU starting with primitive gates And, Or and Not
- Combinational circuits as acyclic wiring diagrams of primitive gates
- Introduction to BSV
 - Intro to types enum, typedefs, numeric types, int#(32) vs integer, bool vs bit#(1), vectors
 - Simple operations: concatenation, conditionals, loops
 - Functions

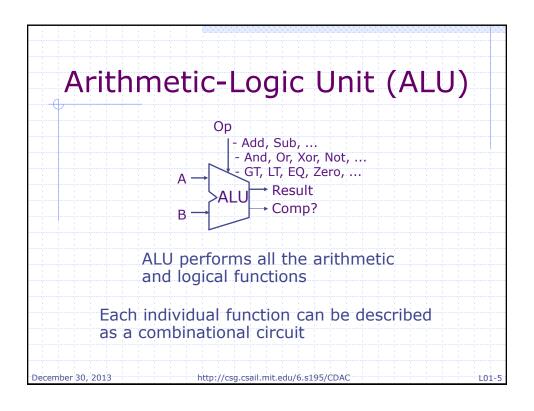
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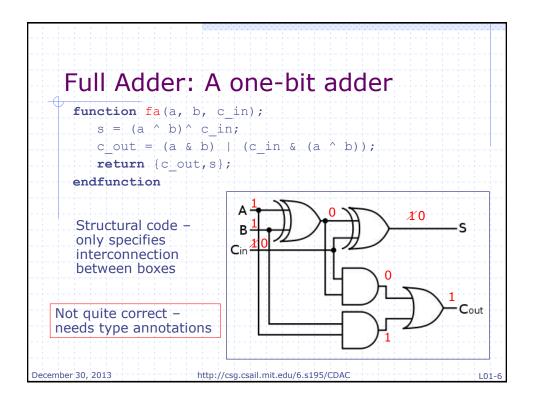
 Static elaboration and a structural interpretation of the textual code

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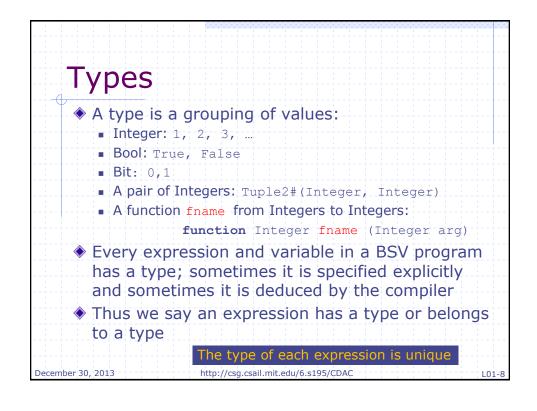
Combinational circuits are acyclic interconnections of gates And, Or, Not Nand, Nor, Xor

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```
Full Adder: A one-bit adder
corrected
function Bit#(2) fa(Bit#(1) a, Bit#(1) b,
                                       Bit#(1) c in);
    Bit \# (1) s = (a ^ b) ^ c_in;
    Bit#(1) c out = (a \& b) | (c in \& (a \land b));
    return {c out,s};
endfunction
 "Bit#(1) a" type
 declaration says that
 a is one bit wide
                       Cin
 {c out,s} represents
 bit concatenation
 How big is {c out,s}?
               2 bits
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```




```
Type synonyms

typedef bit [7:0] Byte;
The same

typedef Bit#(8) Byte;

typedef Bit#(32) Word;

typedef Tuple2#(a,a) Pair#(type a);

typedef Int#(n) MyInt#(type n);

The same

typedef Int#(n) MyInt#(numeric type n);
```

Type declaration versus deduction

- The programmer writes down types of some expressions in a program and the compiler deduces the types of the rest of expressions
- If the type deduction cannot be performed or the type declarations are inconsistent then the compiler complains

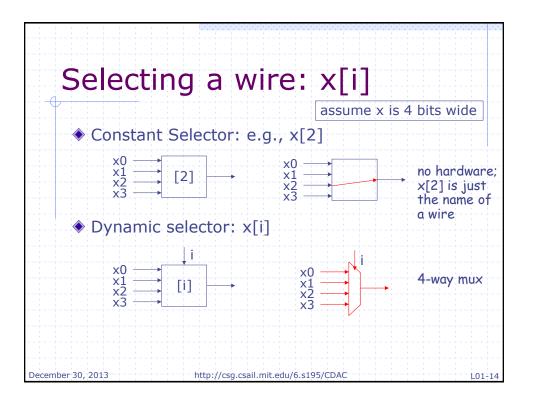
Type checking prevents lots of silly mistakes

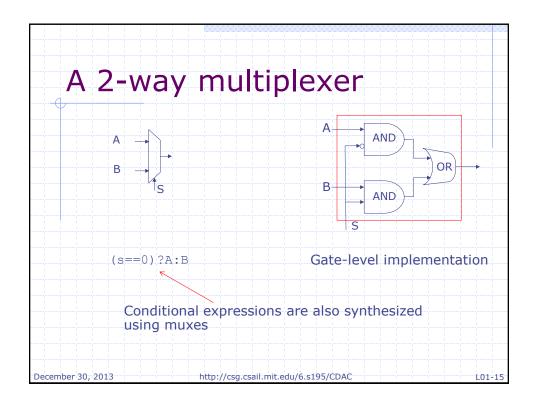
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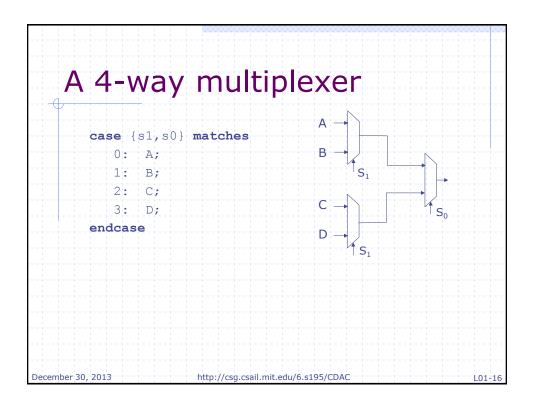
2-bit Ripple-Carry Adder x[0] | y[0] | x[1] | y[1]fa can be used as a black-box long as we c[0] * c[2] understand its type signature s[0] s[1] function Bit#(3) add(Bit#(2) x, Bit#(2) y, Bit#(1) c0); Bit#(3) c=0; c[0] = c0; Bit#(2) s = 0;**let** cs0 = fa(x[0], y[0], c[0]);c[1] = cs0[1]; cs[0] = cs0[0];**let** cs1 = fa(x[1], y[1], c[1]);c[2] = cs1[1]; s[1] = cs1[0];The "let" syntax avoids having **return** {c[2],s}; to write down types explicitly endfunction http://csg.csail.mit.edu/6.s195/CDAC December 30, 2013

```
"let" syntax

The "let" syntax: avoids having to write down types explicitly
■ let cs0 = fa(x[0], y[0], c[0]); The same
■ Bits#(2) cs0 = fa(x[0], y[0], c[0]);
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```





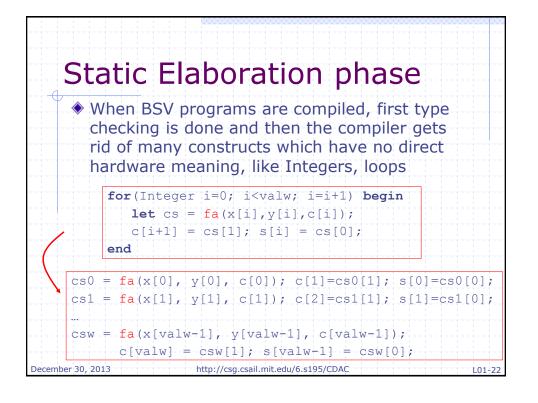


```
An w-bit Ripple-Carry Adder
     function Bit#(w+1) addN(Bit#(w) x, Bit#(w) y,
                                             Bit#(1) c0);
        Bit#(w) s; Bit#(w+1) c=0; c[0] = c0;
        for(Integer i=0; i<w; i=i+1)</pre>
        begin
                                               Not quite correct
            let cs = fa(x[i],y[i],c[i]);
            c[i+1] = cs[1]; s[i] = cs[0];
                                         Unfold the loop to get
     return {c[w],s};
                                         the wiring diagram
     endfunction
                        x[1] y[1]
                                           x[w-1] y[w-1]
                y[0]
           x[0]
                                    c[2] c[w-1
     c[0]
                       s[0]
                                     s[1]
                                                          s[w-1]
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```

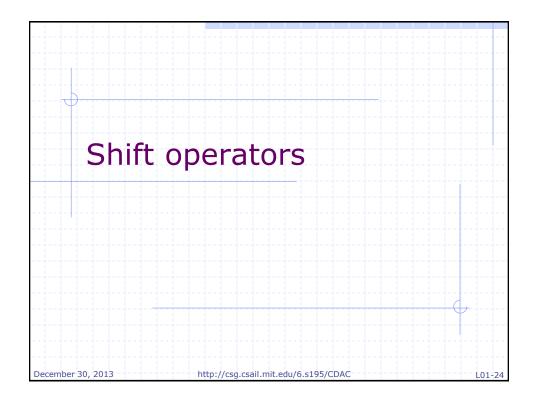
valueOf(w) versus w	
 Each expression has a type and these come from two entirely di w in Bit#(w) resides in the type 	sjoint worlds
Sometimes we need to use values from the types world into actual computation. The function valueOf allows us to do that	
■ Thus	
i <w correct<="" is="" not="" td="" type=""><th></th></w>	
i <valueof(w) correct<="" is="" td="" type=""><th></th></valueof(w)>	
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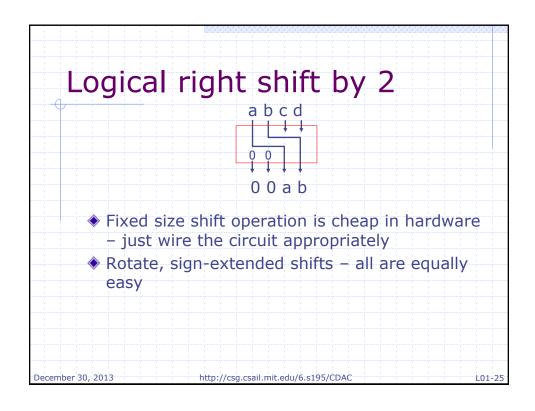
TAdd# (w, 1) Versus w+1 ◆ Sometimes we need to perform operations in the types world that are very similar to the operations in the value world ■ Examples: Add, Mul, Log ◆ We define a few special operators in the types world for such operations ■ Examples: TAdd# (m, n), TMul# (m, n), ...

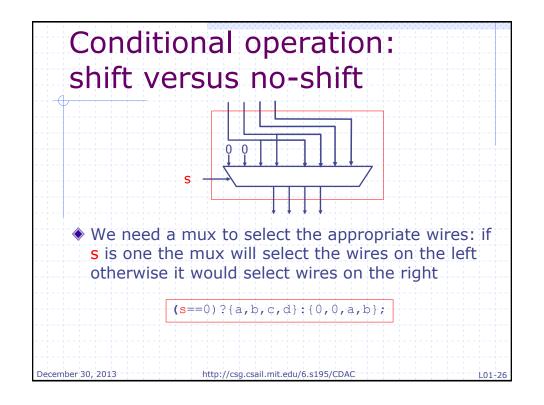
```
A w-bit Ripple-Carry Adder
corrected
 function Bit # (TAdd# (w, 1)) addN (Bit # (w) x, Bit # (w) y,
                                         Bit#(1) c0);
    Bit#(w) s; Bit#(TAdd#(w,1)) c; c[0] = c0;
    let valw ≠ valueOf(w);
                                            → types world
    for(Integer i=0; i<valw; i=i+1)</pre>
                                              equivalent of w+1
    begin
        let cs = fa(x[i],y[i],c[i]);
                                             Lifting a type
        c[i+1] = cs[1]; s[i] = cs[0];
                                              into the value
                                              world
 return {c[valw],s};
 endfunction
       Structural interpretation of a loop – unfold it to
       generate an acyclic graph
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```

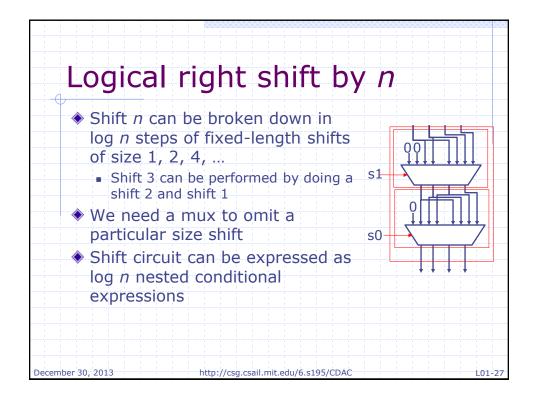


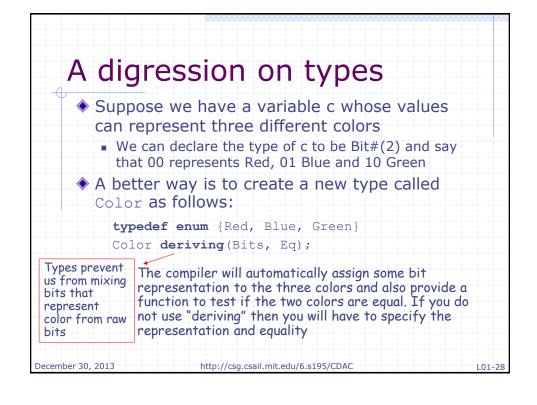
Integer versus Int# (32) In mathematics integers are unbounded but in computer systems integers always have a fixed size BSV allows us to express both types of integers, though unbounded integers are used only as a programming convenience for(Integer i=0; i<valw; i=i+1) begin let cs = fa(x[i],y[i],c[i]); c[i+1] = cs[1]; s[i] = cs[0]; end December 30, 2013 http://csg.csail.mit.edu/6.s195/CDAC L01-23











```
Enumerated types

typedef enum {Red, Blue, Green}
Color deriving(Bits, Eq);

typedef enum {Eq, Neq, Le, Lt, Ge, Gt, AT, NT}
BrFunc deriving(Bits, Eq);

typedef enum {Add, Sub, And, Or, Xor, Nor, Slt, Sltu, LShift, RShift, Sra}
AluFunc deriving(Bits, Eq);

Each enumerated type defines a new type
```

```
Combinational ALU
     function Data alu (Data a, Data b, AluFunc func);
       Data res = case(func)
                                  Given an implementation of
          Add: (a + b);
                                  the primitive operations like
          Sub
               : (a - b);
                                  addN, Shift, etc. the ALU
          And
               : (a & b);
                                  can be implemented simply
               : (a | b);
                                  by introducing a mux
          Or
                                  controlled by op to select the
               : (a ^ b);
          Xor
                                  appropriate circuit
          Nor : ~ (a | b);
          Slt : zeroExtend( pack( signedLT(a, b) ) );
          Sltu : zeroExtend( pack( a < b ) );</pre>
          LShift: (a << b[4:0]);
          RShift: (a >> b[4:0]);
               : signedShiftRight(a, b[4:0]);
          Sra
       endcase;
       return res;
     endfunction
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```

```
Comparison operators
function Bool aluBr(Data a, Data b, BrFunc brFunc);
Bool brTaken = case(brFunc)
Eq : (a == b);
Neq : (a != b);
Le : signedLE(a, 0);
Lt : signedLE(a, 0);
Ge : signedGE(a, 0);
Gt : signedGT(a, 0);
AT : True;
NT : False;
endcase;
return brTaken;
endfunction
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```

